

On the security of group communication schemes

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Secure group communications are a mechanism facilitating protected transmission of messages from a sender to multiple receivers, and many emerging applications in both wired and wireless networks need the support of such a mechanism. There have been many secure group communication schemes in wired networks, which can be directly adopted in, or appropriately adapted to, wireless networks such as mobile ad hoc networks (MANETs) and sensor networks. In this paper we show that the popular group communication schemes that we have examined are vulnerable to the following attack: An outside adversary who compromises a certain legitimate group member could obtain *all* past and present group keys (and thus all the messages protected by them); this is in sharp contrast to the widely-accepted belief that a such adversary can only obtain the present group key (and thus the messages protected by it). In order to understand and deal with the attack, we formalize two security models for stateful and stateless group communication schemes. We show that some practical methods can make a *subclass* of existing group communication schemes immune to the attack.

Keywords: Security, key management, group communication, multicast

1. Introduction

Secure group communications are useful in both wired and wireless networks, because they facilitate protected transmission of messages from a sender to multiple receivers. One important property of secure group communications is to ensure that only the legitimate members (or users, receivers) can have access to the multicast or broadcast data. There have been many secure group communication schemes in the setting of wired networks; popular ones include the stateful LKH [27,28] and OFT [2,25] as well as stateless ones [12,22]. These schemes can be directly adopted in, or appropriately adapted to, the setting of wireless networks such as mobile ad hoc networks (MANETs) and sensor networks. The core component of a secure group communication scheme is its key management method. A common feature among these schemes' key management methods is that each user holds a set of keys that are then utilized to help establish some group keys (which are common to all the group members and are used to encrypt actual messages).

In this paper we show that these group communication schemes, or more specifically their key management methods, are subject to the following attack: An outside

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adversary who compromises a certain legitimate group member could obtain *all* past and present group keys (and thus the data encrypted using these keys). This is in sharp contrast to the widely-accepted belief that such an adversary can only obtain the present group key. This attack is powerful also because it provides the adversary the following flexibility: There are potentially many legitimate group members such that compromising any (or a small number) of them leads to the exposure of both past and present group keys. This flexibility may be particularly relevant in the setting of MANETs and sensor networks because they are typically deployed in a small area and the adversary can capture and compromise the easiest-to-obtain node(s).

1.1. Motivating problems

Now we explore some attack scenarios against the stateful LKH [27,28] and OFT [2,25], and against stateless ones [12,22]. The emphasis is on the case of LKH.

Vulnerability of the LKH and LKH+ schemes: Let's first briefly review the LKH group communication scheme. Following the notations of [28], we let

$$x \rightarrow \{y_1, \dots, y_\ell\} : \{z\}_w$$

denote that x sends the users y_1, \dots, y_ℓ (via multicast or unicast) the encryption of plaintext z using key w , namely the ciphertext $\{z\}_w$.

Consider the simple scenario, as shown in Fig. 1(a), of a group consisting of a key server s and users u_1, \dots, u_8 . The server is responsible for initiating and maintaining the group in the presence of user dynamics (i.e., joins and leaves). The keys are organized as a *key tree*, where the leaves are the users and the inner nodes are the keys. Moreover, each user holds the keys corresponding to the inner nodes on the path starting from the parent of the user and ending at the root. For example, in Fig. 1(a), user u_1 holds keys k_1, k_{123} , and k_{1-8} , where k_{1-8} is the *group key* that can be used to encrypt the communications within the group.

In order to maintain secure communications, each join or leave would require the key server to change some keys that also need to be securely distributed to certain users (via some *rekeying messages*). Ignoring for a moment certain details such as authorization of joining the group and authentication of the messages sent by the key server, in what follows we explain how the key server responds to group dynamics.

After granting a join request from user u_9 , server s shares a key k_9 with user u_9 . Certain keys need to be changed and sent to certain relevant users. As shown in Fig. 1(b), in order to prevent u_9 from accessing past communications, k_{78} and k_{1-8} are changed to k_{789} and k_{1-9} , respectively. Moreover, the new group key k_{1-9} needs to be securely sent to users u_1, \dots, u_9 , and k_{789} needs to be securely sent to users u_7, u_8 , and u_9 . One efficient way to do this is the following algorithm (which corresponds to the so-called *group-oriented rekeying* strategy):

$$\begin{aligned} s &\rightarrow \{u_1, \dots, u_8\} : \{k_{1-9}\}_{k_{1-8}}, \{k_{789}\}_{k_{78}} \\ s &\rightarrow \{u_9\} : \{k_{1-9}, k_{789}\}_{k_9} \end{aligned}$$

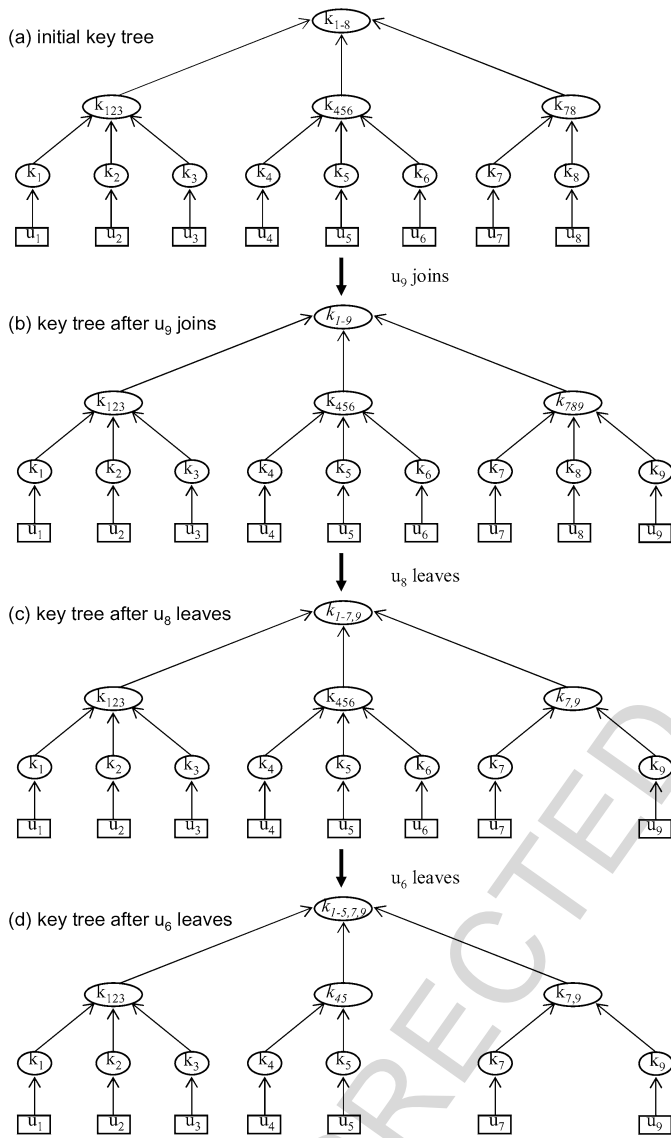


Fig. 1. A scenario of LKH.

Furthermore, k_{1-8} is securely erased by u_1, \dots, u_8 , and k_{78} is securely erased by u_7 and u_8 .

Now suppose u_8 leaves. To prevent u_8 from accessing future communications, as shown in Fig. 1(c), server s needs to change k_{1-9} and k_{789} to $k_{1-7,9}$ and $k_{7,9}$,

1 respectively. Moreover, the new group key $k_{1-7,9}$ needs to be securely sent to users 1
 2 u_1, \dots, u_7, u_9 , and $k_{7,9}$ needs to be securely sent to u_7 and u_9 . One efficient way 2
 3 to do this is the following algorithm (which also corresponds to the group-oriented 3
 4 rekeying strategy): 4

$$5 \quad s \rightarrow \{u_1, \dots, u_7, u_9\} : \{k_{1-7,9}\}_{k_{123}}, \{k_{1-7,9}\}_{k_{456}}, \{k_{1-7,9}\}_{k_{7,9}}, \\ 6 \quad \{k_{7,9}\}_{k_7}, \{k_{7,9}\}_{k_9},$$

7
 8
 9 Furthermore, k_{1-9} is securely erased by u_1, \dots, u_7, u_9 , and k_{789} is securely erased 10
 11 by u_7 and u_9 . 11

12 Now suppose u_6 leaves also. To prevent u_6 from accessing future communica- 12
 13 tions, as shown in Fig. 1(d), server s needs to change $k_{1-7,9}$ and k_{456} to $k_{1-5,7,9}$ 13
 14 and k_{45} , respectively. Moreover, the new group key $k_{1-5,7,9}$ needs to be securely 14
 15 sent to users $u_1, \dots, u_5, u_7, u_9$, and k_{45} needs to be securely sent to users u_4 and u_5 . 15
 16 One efficient way to do this is the following algorithm (which also corresponds to 16
 17 the group-oriented rekeying strategy): 17

$$18 \quad s \rightarrow \{u_1, \dots, u_5, u_7, u_9\} : \{k_{1-5,7,9}\}_{k_{123}}, \{k_{1-5,7,9}\}_{k_{45}}, \{k_{1-5,7,9}\}_{k_{7,9}}, \\ 19 \quad \{k_{45}\}_{k_4}, \{k_{45}\}_{k_5}.$$

20
 21
 22 Furthermore, $k_{1-7,9}$ is securely erased by $u_1, \dots, u_5, u_7, u_9$, and k_{456} is securely 22
 23 erased by u_4 and u_5 . 23

24 Given the above system setting, let us now examine the consequences of a legiti- 24
 25 mate user being compromised. 25

- 26 • Suppose an adversary compromises user u_9 . It is of course true that the adver- 26
 27 sary is able to obtain the present group key $k_{1-5,7,9}$, no matter how the group 27
 28 rekeying scheme works. Moreover, the adversary can obtain $k_{7,9}$ and k_9 . We 28
 29 observe that the adversary who has recorded the network traffic is also able to 29
 30 obtain the past group keys k_{1-9} and $k_{1-7,9}$, because it can decrypt the messages 30
 31 incurred by the events that u_9 joins the group and that u_8 leaves the group: 31
 32

$$33 \quad s \rightarrow \{u_9\} : \{k_{1-9}, k_{789}\}_{k_9}, \\ 34 \quad s \rightarrow \{u_1, \dots, u_7, u_9\} : \{k_{1-7,9}\}_{k_{123}}, \{k_{1-7,9}\}_{k_{456}}, \\ 35 \quad \{k_{1-7,9}\}_{k_{7,9}}, \{k_{7,9}\}_{k_7}, \{k_{7,9}\}_{k_9}.$$

36
 37
 38 We stress that this is true even though the past group keys $k_{1,9}$ and $k_{1-7,9}$ 38
 39 were securely erased by u_9 . As a consequence, the adversary can decrypt the 39
 40 communications encrypted using the past and present group keys k_{1-9} , $k_{1-7,9}$, 40
 41 and $k_{1-5,7,9}$. We notice that the initial group key k_{1-8} is never accessible to u_9 . 41

- 42 • Suppose an adversary compromises user u_7 . Then, the adversary knows 42
 43 $k_{1-5,7,9}$, $k_{7,9}$, and k_7 . Note that the adversary can obtain $k_{1-7,9}$ from the 43

1 recorded traffic corresponding to the event that u_8 leaves the group: 1

$$2 \quad s \rightarrow \{u_1, \dots, u_7, u_9\} : \{k_{1-7,9}\}_{k_{123}}, \{k_{1-7,9}\}_{k_{456}}, \{k_{1-7,9}\}_{k_{7,9}}, \\ 3 \quad \{k_{7,9}\}_{k_7}, \{k_{7,9}\}_{k_9}. \quad 4$$

5
6 We stress that this is true even though the past group key $k_{1-7,9}$ was securely 6
7 erased by u_7 . We notice that the above analysis is based on the implicit assumption 7
8 that the initial group key k_{1-8} was “magically” sent to u_7 . In practice, k_{1-8} 8
9 might have been sent to u_7 via its individual key k_7 . This means that the adversary 9
10 can obtain k_{1-8} , and thus k_{1-9} through the recorded traffic corresponding 10
11 to the event that u_9 joins the group: 11

$$12 \quad s \rightarrow \{u_1, \dots, u_8\} : \{k_{1-9}\}_{k_{1-8}}, \{k_{789}\}_{k_{78}}. \quad 13$$

14 As a consequence, *all* past and present group keys, namely k_{1-8} , k_{1-9} , $k_{1-7,9}$ 15
16 and $k_{1-5,7,9}$, are compromised even if the first three were securely erased by u_7 . 16

- 17 • Suppose u_5 is compromised. Then, the adversary knows $k_{1-5,7,9}$, k_{45} , and k_5 . 17
18 Further, if k_{1-8} was sent to u_5 through an encryption using its individual key k_5 , 18
19 then k_{1-8} is exposed. Moreover, k_{1-9} can be obtained by the adversary from 19
20 the recorded traffic corresponding to the event that u_9 joins the group: 20

$$21 \quad s \rightarrow \{u_1, \dots, u_8\} : \{k_{1-9}\}_{k_{1-8}}, \{k_{789}\}_{k_{78}}. \quad 21$$

22 As a consequence, the past and present group keys, namely k_{1-8} , k_{1-9} and 23
24 $k_{1-5,7,9}$ are compromised, even if they were securely erased by u_5 . 24

25 A similar analysis applies to the case that u_4 is compromised. 25

- 26 • Suppose u_1 is compromised. Then $k_{1-5,7,9}$, k_{123} , and k_1 are obtained by the 26
27 adversary. This means that the adversary can further obtain $k_{1-7,9}$ from the 27
28 recorded traffic corresponding to the event that u_8 leaves the group: 28

$$29 \quad s \rightarrow \{u_1, \dots, u_7, u_9\} : \{k_{1-7,9}\}_{k_{123}}, \{k_{1-7,9}\}_{k_{456}}, \{k_{1-7,9}\}_{k_{7,9}}, \\ 30 \quad \{k_{7,9}\}_{k_7}, \{k_{7,9}\}_{k_9}. \quad 31$$

32 Further, the above analysis is based on the implicit assumption that the 33
34 initial group key k_{1-8} was “magically” sent to u_1 . In practice, k_{1-8} might have 34
35 been sent to u_1 via its individual key k_1 . This means that the adversary can obtain 35
36 k_{1-8} , and thus k_{1-9} through the recorded traffic corresponding to the event 36
37 that u_9 joins the group: 37

$$38 \quad s \rightarrow \{u_1, \dots, u_8\} : \{k_{1-9}\}_{k_{1-8}}, \{k_{789}\}_{k_{78}}. \quad 39$$

40 As a consequence, *all* past and present group keys, namely k_{1-8} , k_{1-9} , $k_{1-7,9}$ 41
42 and $k_{1-5,7,9}$, are compromised even if the first three were securely erased by u_1 . 42

43 A similar analysis applies to the case that u_2 or u_3 is compromised. 43

In summary, the above discussion shows, in sharp contrast to the desired property that the adversary can only obtain the present group key $k_{1-5,7,9}$, that compromising any of u_1, u_2, u_3, u_7 could lead to the exposure of all past and present group keys, and compromising any of u_4, u_5, u_9 leads to the exposure of most past and present group keys. This means that the adversary has considerable flexibility in selecting the *weakest* node(s) to compromise. Finally, we remark that the attack is not fundamentally related to the group-oriented rekeying strategy, and that LKH+ [26], which was seemingly motivated from an efficiency perspective, resolves only a piece of the problem because the above attack remains effective when the group dynamics are incurred by leaving events.

Remark 1. While there could be other methods to bootstrap the initial keys (e.g., k_{1-8} is not protected by k_7), the following scenario would still support the above conclusion. Suppose at system initialization there is no user but the server, then users join the system one by one via LKH's join protocol (cf. Appendix A). In this case, transmission of group keys is always protected by individual keys, meaning that compromise of some user (or users) could lead to the exposure of all past and present group keys.

Remark 2. One may observe that the compromise of past group keys may not be a serious problem. This is so because if a node stored all the past communication content, it will be leaked to the adversary when the node is compromised. However, there are situations, such as sensitive applications, where the nodes do not, or even are not allowed to, store past communication content. We notice that this issue is also relevant to [4,7].

Vulnerability of the One-way Function Tree (OFT) scheme: OFT [2,25] is a stateful group communication scheme. The basic idea underlying the OFT scheme is the following (we refer the reader to [2,25] for details). The center maintains a binary tree, each node x of which is associated with two cryptographic keys: a node key k_x and a blinded node key $k'_x = g(k_x)$, where g is an appropriate one-way function. Every leaf of the tree is associated with a group member, and the center assigns a randomly chosen key k_x to each member x . Let f be a "mixing" function (e.g., \oplus). The interior node keys are defined by the rule

$$k_u = f(g(k_{left(u)}), g(k_{right(u)}))$$

where $left(u)$ and $right(u)$ are the left and right children of the node u , respectively. This way, the node key associated with the root of the tree is the group key. In order for a member u to derive the group key, the center (or server, sender) sends the blinded node keys of nodes adjacent to the nodes on (i.e., of the nodes "hanging off) the path from u to the root.

1 When a new member joins the group, an existing leaf node u is split, the member 1
 2 associated with u is now associated with $left(u)$, and the new member is associated 2
 3 with $right(u)$. Both members are given new keys. The new blinded node keys that 3
 4 have been changed are *securely sent* to the appropriate subgroups of members. 4

5 When the member associated with a node u is evicted from the group, the member 5
 6 assigned to the sibling of u is reassigned to the parent p of u and given a new leaf 6
 7 key. If the sibling s of u is the root of a subtree, then p becomes s , moving the subtree 7
 8 closer to the root, and one of the leaves of this subtree is given a new key. The new 8
 9 blinded node keys are *securely sent* to the appropriate subgroups of members. 9

10 Now we show why the OFT scheme is also vulnerable to a similar attack. The key 10
 11 observation is that whenever there is a change to any blinded node key, the center 11
 12 needs to *securely send* the new blinded node keys to certain other legitimate nodes. 12
 13 It seems that any reasonable method would be based on the keys possessed by the 13
 14 respective nodes (e.g., u). Since u can derive the new group key after receiving the 14
 15 rekeying message, an *outsider* adversary could use the following strategy to recover 15
 16 the group key: it first records the rekeying message, and then breaks into u 's com- 16
 17 puter *after* the next rekeying event (assuming that u is still legitimate). Moreover, 17
 18 compromising any of the nodes that have not been evicted enables the adversary to 18
 19 recover past and present group keys. 19
 20

21 **Vulnerability of the stateless subset-cover framework:** Naor et al. [22] presented 21
 22 the first practical stateless group communication scheme, which has its roots in 22
 23 broadcast encryption [9]. Compared with the stateful group communication schemes 23
 24 discussed above, stateless schemes have the nice feature that they do not assume 24
 25 the receivers (or users, members) being always on-line. Since the receivers do not 25
 26 necessarily update their state from session to session, stateless schemes are especially 26
 27 good for applications over lossy channels (e.g., MANETs and sensor networks). We 27
 28 stress that the security analysis presented in [22] remains sound in its adversarial 28
 29 model; whereas the present paper considers a strictly stronger adversarial model. 29

30 The subset-cover framework of [22] is reviewed in Fig. 2, where \mathcal{N} is the set 30
 31 of all users, $\mathcal{R} \subset \mathcal{N}$ is a group of $|\mathcal{R}| = r$ users whose decryption privileges 31
 32 should be revoked, and E_L and F_K are two appropriate symmetric key cryptosys- 32
 33 tems (whose properties will be specified later). The goal of a stateless group com- 33
 34 munication scheme is to allow a center to transmit a message M to all users such 34
 35 that any user $u \in \mathcal{N} \setminus \mathcal{R}$ can decrypt the message correctly, while even a coalition 35
 36 consisting of all members of \mathcal{R} cannot decrypt it. Suppose S_1, \dots, S_w are a collec- 36
 37 tion of subsets of users, where $S_j \subseteq \mathcal{N}$ for $1 \leq j \leq w$, and each S_j is assigned 37
 38 a long-lived key L_j such that each $u \in S_j$ should be able to deduce L_j from its 38
 39 secret information I_u . Given a revoked set \mathcal{R} , if one can partition $\mathcal{N} \setminus \mathcal{R}$ into (ideally 39
 40 disjoint) sets S_{i_1}, \dots, S_{i_m} such that $\mathcal{N} \setminus \mathcal{R} \subseteq \cup_{\ell=1}^m S_{i_\ell}$, then a session key K can be 40
 41 encrypted m times with L_{i_1}, \dots, L_{i_m} , and each user $u \in \mathcal{N} \setminus \mathcal{R}$ can obtain K and 41
 42 thus M . 42
 43

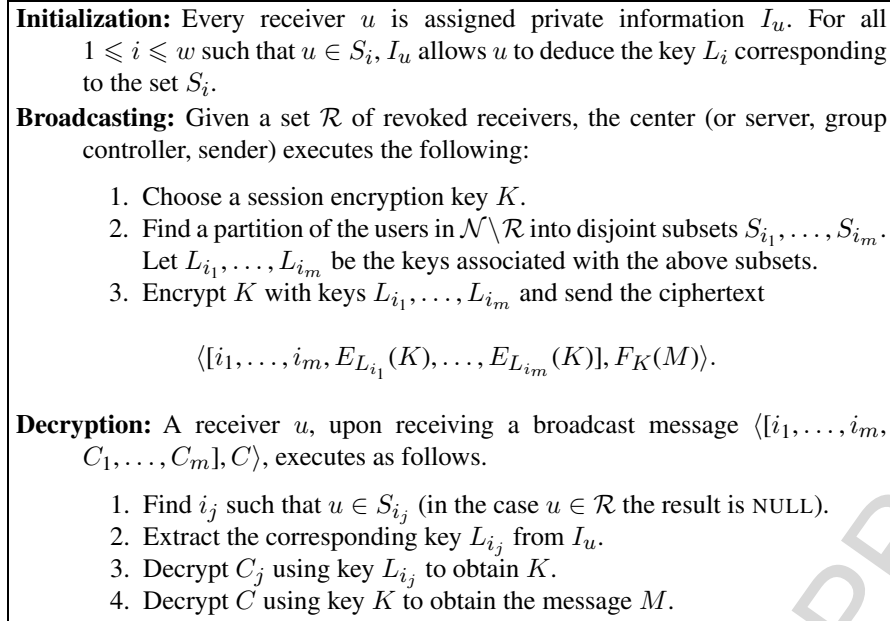


Fig. 2. The subset-cover revocation framework.

The subset-cover framework has a vulnerability similar to the one against the stateful group schemes. Specifically, suppose an adversary $\mathcal{A} \notin \mathcal{N}$ records all the encrypted communications over the channels. If \mathcal{A} breaks into a legitimate user $u \in \mathcal{N}$ at a later point in time, then \mathcal{A} obtains I_u , which allows it to recover the L_{i_j} (and thus the encrypted M) that u was entitled to obtain. In the extreme case that u has never been revoked, \mathcal{A} can recover all past and present keys.

1.2. Our contributions

We trace the above vulnerability of group communication schemes back to that their security models (if any) are not sufficient. We formalize two adversarial models. One is called the *passive attack model*, in which the adversary is passive in the sense that it is only allowed to join and leave the group in an arbitrary fashion, but not allowed to corrupt any legitimate members. This model has seemingly been implicitly adopted in the existing group communication literature. The other more realistic one is called the *active outsider attack model*, in which the adversary is further allowed to corrupt legitimate members. This model aids understanding and dealing with the aforementioned attack. In each of the two models, we define two security notions, namely *forward-security* meaning that the revoked or evicted members, even if they collude, cannot obtain the future group keys, and *backward-security* mean-

ing that a newly admitted member cannot obtain the past group keys.¹ This allows us to obtain the following interesting results about the relationships between these security notions, which are equally applicable to both stateful and stateless group communication schemes (see Sections 3.3 and 6.2, respectively).

1. In the active outsider attack model, backward-security (also called *strong-security*) is *strictly* stronger than forward-security (also called *security*). This means that in the active outsider attack model one only needs to prove the backward-security property.
2. In the passive attack model, backward-security is equivalent to forward-security.
3. Backward-security in the active outsider attack model (i.e., *strong-security*) is *strictly* stronger than backward-security in the passive attack model. However, we do *not* know whether forward-security in the active outsider attack model is also *strictly* stronger than its counterpart in the passive attack model (we only know that when the adversary is *static* they are equivalent).
4. The security achieved in existing group communication schemes (e.g., [12, 22,25,28]) is indeed, as we will show, forward-security in the active outsider attack model (i.e., *security*). This has not become clear until now because there were no formal models specified before (in spite of the fact that the passive attack model has seemingly been implicitly adopted in the literature). The achieved *security* property is at least as strong as what we call backward-security in the passive attack model, but *strictly* weaker than what we call backward-security in the active outsider attack model (i.e., *strong-security*) – a property that blocks the attack discussed above.

Besides the above general results, we show that some practical methods can transform a *subclass* of the group communication schemes (including LKH [27,28], LKH+ [26], and the complete subtree method [22]) into ones that achieve the desired *strong-security*. The methods are based on two general compilers. The extra complexity imposed by the compilers is typically that at each rekeying event a group member conducts logarithmically-many pseudorandom function evaluations. This should not jeopardize their utility even in the setting of MANETs and sensor networks, as pseudorandom functions may be implemented with block ciphers in practice. We also present instantiations of the compilers, which lead to concrete schemes that achieve the desired *strong-security*.

Although the technical means underlying the transformation is to evolve the keys based on a secure pseudorandom function family – an idea inspired by [4], there are some subtle issues in our settings. First, we must allow the adversary to corrupt some group keys that are used to encrypt the communications *before* the rekeying

¹The terms follow the group communication literature (see, e.g., [27,28]). Their meanings are indeed different from the ones adopted in the cryptographic literature [1,3,4].

1 message of interest. Of course, the corrupt members must have been revoked before
2 that rekeying message. On the other hand, in [4] no such corruption is allowed before
3 the event of interest. Second, from an adversary's perspective, there could be many
4 "valuable" users in our settings, meaning that an adversary only needs to compromise
5 the *weakest* one(s) of them. Whereas, no such flexibility is given to the adversary in
6 the setting of [4].

8 1.3. Related work

10 LKH was independently invented in [27,28]. Although these schemes are mainly
11 invented for secure multicast applications, we believe that many other applications
12 can utilize such a scheme; we refer the reader to [6,23] for a survey, including the
13 relationship between the schemes of [27,28] and the schemes of [9,22]. We notice
14 that the stateless schemes (e.g., [12,22]) are perhaps more useful in an environment
15 of lossy channels. Although the LKH scheme has been extended in several direc-
16 tions, these extensions are motivated to improve performance rather than to achieve
17 strictly stronger security. For example, performance can be improved by periodic
18 group rekeying [24] or batch rekeying [19], and improved trade-offs between stor-
19 age and communication are available in [6,8,21]. Nevertheless, these techniques may
20 also be utilized in our *strongly-secure* group communication schemes. To the
21 best of our knowledge, our work is the first one that identifies a new and realistic
22 attack, and presents solutions for (a subclass of) the popular group communication
23 schemes. The variant presented in [26] (which is also known as LKH+) is similar
24 to our performance optimization in that the communication complexity incurred by
25 joining events can be substantially reduced. However, there was no formal treatment
26 of the utilized key evolution, nor was their scheme resistant against the attack in-
27 troduced in Section 1.1.

28 While secure group-oriented communications have been extensively investigated
29 in the setting of wired networks, their counterparts in the setting of wireless networks
30 have yet to be thoroughly explored. Although the aforementioned schemes can be di-
31 rectly deployed in wireless settings, a simple-minded adoption may not lead to the
32 desired performance (see, e.g., [17,31]). Fortunately, there have been some inter-
33 esting investigations that show that these schemes can be adapted (e.g., by taking
34 into account some physical characteristics of ad hoc networks [15–18]) so that bet-
35 ter performance can be achieved. One of the practical values of the present paper is
36 that the significantly improved security guarantee in the popular group communica-
37 tion schemes can be seamlessly integrated into the methods for improving perfor-
38 mance [15–18]. Indeed, our schemes can be easily integrated into any other methods
39 for improving performance to achieve better security, as long as the methods assume
40 "black-box" access to an underlying security group communication scheme. There
41 have been a few other attempts at securing group communications in such settings:
42 [14] presented a scheme for secure multicast communications in MANETs based
43

1 on public key cryptosystems; [31] investigated a different approach to secure group 1
2 communications.

3 A similar study on enhancing security of public key cryptography based broadcast 3
4 encryption was investigated in [30]. 4
5

6 1.4. Outline 6

7
8 The rest of the paper is organized as follows. In Section 2 we briefly review some 8
9 cryptographic preliminaries. In Section 3 we present formal models and security 9
10 definitions of stateful group communication schemes, as well as the relationships 10
11 between the security notions. In Section 4 we present a compiler for stateful group 11
12 communication schemes and investigate its properties. The compiler is utilized in 12
13 Section 5 to derive a concrete *strongly-secure* stateful group communication 13
14 scheme from the merely *secure* LKH, which is reviewed in Appendix A for com- 14
15 pleteness. In Section 6 we explore stateless group communication schemes in parallel 15
16 to their stateful counterparts. We conclude the paper in Section 7. 16
17

18 2. Cryptographic preliminaries 18

19
20 A function $\epsilon: \mathbb{N} \rightarrow \mathbb{R}^+$ is *negligible* if $\forall c \exists \kappa_c$ s.t. $\forall \kappa > \kappa_c$, we have $\epsilon(\kappa) < 1/\kappa^c$. 20
21

22 We will base security of group communication schemes on the security of pseudo- 22
23 random function families. For a security parameter κ , a pseudorandom function 23
24 (PRF) family $\{f_k\}$ parameterized by a secret value $k \in_R \{0, 1\}^\kappa$ has the following 24
25 property [10]: A probabilistic polynomial-time adversary \mathcal{A} has only a negligible 25
26 (in κ) advantage in distinguishing f_k from a perfect random function (with the same 26
27 domain and range). It is well-known that pseudorandom functions can be naturally 27
28 used to construct symmetric key encryption schemes that are secure against chosen- 28
29 plaintext attacks (which suffices for our treatment of LKH). Informally, this means 29
30 that no adversary is able to learn any significant information about the encrypted 30
31 content. We refer the reader to [13] for a thorough treatment on this subject. 31
32
33

34 **Definition 2.1** (computational independence). Consider a set $S = \{s_1, \dots, s_\ell\}$ of 34
35 secret binary strings of length κ , where $\ell = \text{poly}(\kappa)$ for some polynomial poly . We 35
36 say s_1, \dots, s_ℓ are computationally independent of each other if for any probabilistic 36
37 polynomial-time algorithm \mathcal{A} , 37
38

$$39 \quad |\Pr[\mathcal{A}(s_1, \dots, s_\ell) \text{ returns "real"}] - \Pr[\mathcal{A}(r_1, \dots, r_\ell) \text{ returns "real"}]| = \epsilon(\kappa) 39$$

40 where $r_1, \dots, r_\ell \in_R \{0, 1\}^\kappa$ are uniformly drawn at random, and ϵ is a negligible 40
41 function. 41
42
43

3. Model and definition of stateful secure group communications

In Section 3.1 we present a formal security model for stateful (and symmetric key cryptography based) group communications. In Section 3.2 we specify the adversarial models and desired security properties. In Section 3.3 we explore the relationships between the security notions.

3.1. Model

Let κ be a security parameter, and \mathbb{ID} be the set of possible group members (i.e., users, receivers, or principals) such that $|\mathbb{ID}|$ is polynomially-bounded in κ . There is a special entity called a *Group Controller* (i.e., key server, center, server, or sender), denoted by \mathcal{GC} , such that $\mathcal{GC} \notin \mathbb{ID}$.

Since a stateful group communication scheme is driven by “rekeying” events (because of joining or leaving operations below), it is convenient to treat the events as occurring at “virtual time” $t = 0, 1, 2, \dots$, because the group controller is able to maintain such an execution history. This indeed accommodates the following important two cases: (1) all the parties periodically update their keys, even if there are no joining or leaving operations – this is relevant when a scheme achieves what we call *strong-security* specified below; (2) the lengths of the time periods do not have to be the same – this is the case when the rekeying events occur in an arbitrary fashion. At time t , let $\Delta^{(t)}$ denote the set of legitimate group members, $k^{(t)} = k_{\mathcal{GC}}^{(t)} = k_{U_1}^{(t)} = \dots$ the group key,² $K_{\mathcal{GC}}^{(t)}$ the set of keys held by the \mathcal{GC} , $K_U^{(t)}$ the set of keys held by $U \in \Delta^{(t)}$, and $\text{acc}_U^{(t)}$ the state indicating whether $U \in \Delta^{(t)}$ has successfully received the rekeying message. Initially, $\forall U \in \mathbb{ID}, t \in \mathbb{N}$, set $\text{acc}_U^{(t)} \leftarrow \text{FALSE}$. We assume that the \mathcal{GC} treats joining and leaving operation separately (e.g., first fulfilling the leaving operation and then immediately the joining one), even if the requests are made simultaneously. This strategy has indeed been adopted in the group communication literature.

To simplify the presentation, we assume that during the system initialization (i.e., *Setup* below) or the admission of a joining user, the \mathcal{GC} can communicate with each legitimate member $U \in \mathbb{ID}$ through an *authenticated private* channel, and that after the system initialization the \mathcal{GC} can communicate with any U through an *authenticated* channel. We notice that authenticated channels can be implemented by a digital signature scheme [28], and digital signatures are sometimes necessary [5].

We will not make any *synchronization* assumption about the underlying communication model, which could therefore be asynchronous [20]. However, known practical schemes (e.g., [8,27,28]) assume *reliable* delivery, which would require some (loose) clock synchronization.

²It is also known as a session key in the group communication literature.

1 A group communication scheme has the following components: 1

2
3 **Setup:** The group controller \mathcal{GC} generates a set of keys $K_{\mathcal{GC}}^{(0)}$, and distributes ap- 2
4 propriate subsets of $K_{\mathcal{GC}}^{(0)}$ to the present group members (that may be deter- 3
5 mined by the adversary), $\Delta^{(0)} \subseteq \mathbb{ID}$, through the authenticated private chan- 4
6 nels. Each member $U_i \in \Delta^{(0)}$ holds a set of keys denoted by $K_{U_i}^{(0)} \subset K_{\mathcal{GC}}^{(0)}$, 5
7 and there is a key, $k^{(0)}$ that is common to all the present members, namely 6
8 $k^{(0)} \in K_{\mathcal{GC}}^{(0)} \cap K_{U_1}^{(0)} \cap \dots \cap K_{U_{|\Delta^{(0)}|}}^{(0)}$. 7
9

10 **Join:** This algorithm is executed by group controller \mathcal{GC} at time, say, t due to some 10
11 join request(s) (we abstract away the out-of-band authentication and establish- 11
12 ment of an individual key for each of the new members). It takes as input: 12
13 (1) identities of previous group members, $\Delta^{(t-1)}$, (2) identities of newly ad- 13
14 mitted group members, $\Delta' \subseteq \mathbb{ID} \setminus \Delta^{(t-1)}$, (3) keys held by the group con- 14
15 troller, $K_{\mathcal{GC}}^{(t-1)}$, and (4) keys held by group members, $\{K_{U_i}^{(t-1)}\}_{U_i \in \Delta^{(t-1)}} =$ 15
16 $\{K_{U_i}^{(t-1)} : U_i \in \Delta^{(t-1)}\}$. 16
17

18 It outputs updated system state information, including: (1) identities of new 18
19 group members, $\Delta^{(t)} \leftarrow \Delta^{(t-1)} \cup \Delta'$, (2) new keys for the \mathcal{GC} itself, $K_{\mathcal{GC}}^{(t)}$, 19
20 (3) new keys for new group members, $\{K_{U_i}^{(t)}\}_{U_i \in \Delta^{(t)}}$, which are sent to the 20
21 legitimate users through the authenticated channels, (4) new group key $k^{(t)} \in$ 21
22 $K_{\mathcal{GC}}^{(t)} \cap K_{U_1}^{(t)} \cap \dots \cap K_{U_{|\Delta^{(t)}|}}^{(t)}$. 22
23

24 Formally, denote it by $(\Delta^{(t)}, K_{\mathcal{GC}}^{(t)}, \{K_{U_i}^{(t)}\}_{U_i \in \Delta^{(t)}}) \leftarrow \text{Join}(\Delta^{(t-1)}, \Delta', K_{\mathcal{GC}}^{(t-1)},$ 24
25 $\{K_{U_i}^{(t-1)}\}_{U_i \in \Delta^{(t-1)}})$. 25
26

27 **Leave:** This algorithm is executed by the group controller \mathcal{GC} at time, say, t due 27
28 to leave or revocation operation(s). It takes as input: (1) identities of previous 28
29 group members, $\Delta^{(t-1)}$, (2) identities of leaving group members, $\Delta' \subseteq \Delta^{(t-1)}$, 29
30 (3) keys held by the controller, $K_{\mathcal{GC}}^{(t-1)}$, and (4) keys held by group members, 30
31 $\{K_{U_i}^{(t-1)}\}_{U_i \in \Delta^{(t-1)}}$. 31

32 It outputs updated system state information, including: (1) identities of new 32
33 group members, $\Delta^{(t)} \leftarrow \Delta^{(t-1)} \setminus \Delta'$, (2) new keys for \mathcal{GC} , $K_{\mathcal{GC}}^{(t)}$, (3) new keys 33
34 for new group members, $\{K_{U_i}^{(t)}\}_{U_i \in \Delta^{(t)}}$, which are sent to the legitimate users 34
35 through the authenticated channels, (4) a new group key $k^{(t)} \in K_{\mathcal{GC}}^{(t)} \cap K_{U_1}^{(t)} \cap$ 35
36 $\dots \cap K_{U_{|\Delta^{(t)}|}}^{(t)}$. 36
37

38 Formally, denote it by $(\Delta^{(t)}, K_{\mathcal{GC}}^{(t)}, \{K_{U_i}^{(t)}\}_{U_i \in \Delta^{(t)}}) \leftarrow \text{Leave}(\Delta^{(t-1)}, \Delta', K_{\mathcal{GC}}^{(t-1)},$ 38
39 $\{K_{U_i}^{(t-1)}\}_{U_i \in \Delta^{(t-1)}})$. 39
40

41 **Rekey:** This algorithm is executed by the legitimate group members belonging 41
42 to $\Delta^{(t)}$ at time t , where $\Delta^{(t)}$ is derived from a Join or Leave event. Specifically, 42
43 $U_i \in \Delta^{(t)}$ runs this algorithm upon receiving the message from the \mathcal{GC} over the 43

1 authenticated channel. The algorithm takes as input the received message and 1
 2 U_i 's secrets, and is supposed to output the updated keys for the group member. 2
 3 If the execution of the algorithm is successful, U_i sets: (1) $\text{acc}_{U_i}^{(t)} \leftarrow \text{TRUE}$, 3
 4 (2) $K_{U_i}^{(t)}$, where $k_{U_i}^{(t)} \in K_{U_i}^{(t)}$ is supposed to be the new group key. 4
 5

6 If the rekeying event is incurred by a **Join** event, every $U_i \in \Delta^{(t)}$ erases $K_{U_i}^{(t-1)}$ 6
 7 and any temporary storage after obtaining $K_{U_i}^{(t)}$. If the rekeying event is in- 7
 8 curred by a **Leave** event, every $U_i \in \Delta^{(t)}$ erases $K_{U_i}^{(t-1)}$ and any temporary 8
 9 storage after obtaining $K_{U_i}^{(t)}$, and every *honest* leaving group member $U_j \in \Delta'$ 9
 10 erases $K_{U_j}^{(t-1)}$ (although a *corrupt* one does not have to follow this protocol). 10
 11

12 We require that any group communication scheme satisfy the following 12
 13 correctness requirement: for any $t = 1, 2, \dots$ and $\forall U \in \Delta^{(t)}$, if $\text{acc}_U^{(t)} = \text{TRUE}$, 13
 14 then $k_U^{(t)} = k^{(t)}$ and $K_U^{(t)} \subset K_{\mathcal{GC}}^{(t)}$. 14
 15

16 3.2. Security definitions 16

17 We consider an adversary that has complete control over all the communications 17
 18 in the network. To simplify the definition, we assume that the group controller is 18
 19 never compromised; this is not necessarily a restriction because the adversary could 19
 20 have compromised all the group members (and thus have obtained the secrets the 20
 21 group controller holds). 21
 22

23 An adversary's interaction with principals in the network is modeled by allowing 23
 24 it to have access to (some of) the following oracles: 24
 25

- 26 • $\mathcal{O}_{\text{Send}}(U, t, M, \text{action})$: Send a message M to $U \in \{\mathcal{GC}\} \cup \mathbb{ID}$ at time $t \geq 0$, 26
 27 and output its reply, where $\text{action} \in \{\text{Setup}, \text{Join}, \text{Leave}, \text{Rekey}\}$ meaning 27
 28 that U will execute according to the corresponding protocol, and M specifies 28
 29 the needed information for executing the protocol. Of course, the query of type 29
 30 **Setup** is only made at time $t = 0$. 30

31 These oracle accesses are meant to capture that the adversary can observe the 31
 32 reactions of the non-corrupt participants (e.g., the incurred message exchanges). 32
 33 For example, the adversary can let some honest (i.e., non-corrupt) users join or 33
 34 leave the group in question. 34

- 35 • $\mathcal{O}_{\text{Reveal}}(U, t)$: Output the group key held by $U \in \Delta^{(t)}$ at time t , namely $k_U^{(t)}$. 35
- 36 • $\mathcal{O}_{\text{Corrupt}}(U, t)$: Output the keys held by $U \in \Delta^{(t)}$ at time t , namely $K_U^{(t)}$. 36
- 37 • $\mathcal{O}_{\text{Test}}(U, t)$: This oracle may be queried only once, at any time during the adver- 37
 38 sary's execution. A random bit b is generated: if $b = 1$ the adversary is given 38
 39 $k_U^{(t)}$ where $U \in \Delta^{(t)}$, and if $b = 0$ the adversary is given a random key of 39
 40 length $|k_U^{(t)}|$. 40
 41

42 Now we define the *active outsider attack model* that is strictly more powerful than 42
 43 the *passive outsider attack model* that has been implicitly utilized in the literature. 43

Definition 3.1 (active outsider attack model). In this model, the adversary \mathcal{A} may have access to all the oracles specified above. In particular, an “outsider” $\mathcal{A} \notin \Delta^{(t)}$ is allowed to issue an $\mathcal{O}_{Reveal}(U, t)$ or $\mathcal{O}_{Corrupt}(U, t)$ query for some $U \in \Delta^{(t)}$.

Definition 3.2 (passive attack model). In this model, the adversary is only allowed to make $\mathcal{O}_{Send}(\cdot, \cdot, \cdot, \cdot)$ and $\mathcal{O}_{Test}(\cdot, \cdot)$ queries. In other words, the adversary is only allowed to join and leave the group (in an arbitrary fashion though).

In each of the two models, we define two security notions: backward-security and forward-security. This leads to four security notions: (1) forward-security in the active outsider attack model or simply *security*, (2) backward-security in the active outsider attack model or simply *strong-security*, (3) forward-security in the passive attack model, and (4) backward-security in the passive attack model.

Definition 3.3 (*security*). Intuitively, it means that \mathcal{A} learns no information about a group key if (1) with respect to the corresponding rekeying event there is no corrupt legitimate member (this implicitly implies that all the members that were corrupted by \mathcal{A} must have been revoked), and (2) no member is corrupted by \mathcal{A} after the rekeying event. Formally, consider the following event **Succ**:

- (1) The adversary can make arbitrary oracle queries at any time $t_1 < t$, except the following restrictions hold.
- (2) The adversary queries the $\mathcal{O}_{Test}(U, t)$ oracle with $\text{acc}_U^{(t)} = \text{TRUE}$, and correctly guesses the bit b used by the $\mathcal{O}_{Test}(U, t)$ oracle in answering this query.
- (3) There is no $\mathcal{O}_{Reveal}(V, t)$ query for any $V \in \Delta^{(t)}$. (Otherwise, the group key is trivially compromised.)
- (4) For every $\mathcal{O}_{Corrupt}(V, t_1)$ query where $t_1 < t$, there must have been an $\mathcal{O}_{Send}(\mathcal{GC}, t_2, V, \text{Leave})$ query where $t_1 < t_2 \leq t$. This captures that the corrupt members must have been revoked before the rekeying message at time t .
- (5) There is no $\mathcal{O}_{Corrupt}(V, t_3)$ query for any $t_3 \geq t$ and $V \in \Delta^{(t_3)}$.

The advantage of the adversary \mathcal{A} in attacking the group communication scheme is defined as $\text{Adv}_{\mathcal{A}}(\kappa) = |2 \cdot \Pr[\text{Succ}] - 1|$, where $\Pr[\text{Succ}]$ is the probability that the event **Succ** occurs, and the probability is taken over the coins used by \mathcal{GC} and by \mathcal{A} . We say a scheme is *secure* if for all probabilistic polynomial-time adversary \mathcal{A} it holds that $\text{Adv}_{\mathcal{A}}(\kappa)$ is negligible in κ .

Definition 3.4 (*strong-security*). Intuitively, it means that an adversary learns no information about a group key if, with respect to the rekeying event of interest there is no corrupt legitimate member (this implicitly implies that all the previously corrupt members have been revoked). Formally, consider the following event **Succ**:

- (1)–(4) The same as in the definition of *security*.
- (5) There is no $\mathcal{O}_{Corrupt}(V, t_3)$ query for $t_3 = t$ and $V \in \Delta^{(t_3)}$. (This does not rule out that there could be some $\mathcal{O}_{Corrupt}(V, t_3)$ query for $t_3 > t$.)

1 The advantage of the adversary \mathcal{A} in attacking the group communication scheme is 1
 2 defined as $\text{Adv}_{\mathcal{A}}(\kappa) = |2 \cdot \text{Pr}[\text{Succ}] - 1|$, where $\text{Pr}[\text{Succ}]$ is the probability that the 2
 3 event **Succ** occurs, and the probability is taken over the coins used by \mathcal{GC} and by \mathcal{A} . 3
 4 We say a scheme is **strongly-secure** if for all probabilistic polynomial-time 4
 5 adversary \mathcal{A} it holds that $\text{Adv}_{\mathcal{A}}(\kappa)$ is negligible in κ . 5
 6

7 **Definition 3.5** (forward-security in the passive attack model). Intuitively, it means 7
 8 that \mathcal{A} , which is not allowed to make any $\mathcal{O}_{\text{Reveal}}$ or $\mathcal{O}_{\text{Corrupt}}$ query, learns no infor- 8
 9 mation about any group key after leaving the group. Formally, consider the following 9
 10 event **Succ**: 10

- 11 (1) The adversary arbitrarily queries the $\mathcal{O}_{\text{Send}}(\cdot, t_1, \cdot, \cdot)$ oracle for any $t_1 < t$. More- 11
 12 over, the adversary itself can arbitrarily join or leave the group at time t_1 , 12
 13 provided that the following restriction holds. 13
 14 (2) The adversary queries the $\mathcal{O}_{\text{Test}}(U, t)$ oracle, where (1) $\text{acc}_U^{(t)} = \text{TRUE}$ for an 14
 15 honest user U , and (2) $\mathcal{A} \notin \Delta^{(t)}$. Then, the adversary correctly guesses the bit 15
 16 b used by the $\mathcal{O}_{\text{Test}}(U, t)$ oracle in answering this query. 16
 17

18 The advantage of the adversary \mathcal{A} in attacking the group communication scheme is 18
 19 defined as $\text{Adv}_{\mathcal{A}}(\kappa) = |2 \cdot \text{Pr}[\text{Succ}] - 1|$, where $\text{Pr}[\text{Succ}]$ is the probability that the 19
 20 event **Succ** occurs, and the probability is taken over the coins used by \mathcal{GC} and by \mathcal{A} . 20
 21 We say a scheme is **secure** if for all probabilistic polynomial-time adversary \mathcal{A} it 21
 22 holds that $\text{Adv}_{\mathcal{A}}(\kappa)$ is negligible in κ . 22
 23

24 **Definition 3.6** (backward-security in the passive attack model). Intuitively, it means 24
 25 that \mathcal{A} , which is not allowed to make any $\mathcal{O}_{\text{Reveal}}$ or $\mathcal{O}_{\text{Corrupt}}$ query, learns no infor- 25
 26 mation about any group key before joining the group (again). Formally, consider the 26
 27 following event **Succ**: 27
 28

- 29 (1) The adversary may arbitrarily query the $\mathcal{O}_{\text{Send}}(\cdot, t_1, \cdot, \cdot)$ oracle for any $t_1 < t$. 29
 30 Moreover, \mathcal{A} can arbitrarily join or leave the group at time t_1 , provided that 30
 31 the following restriction holds. 31
 32 (2) The adversary queries the $\mathcal{O}_{\text{Test}}(U, t)$ oracle, where (1) $\text{acc}_U^{(t)} = \text{TRUE}$ for an 32
 33 honest user U , and (2) $\mathcal{A} \notin \Delta^{(t)}$. 33
 34 (3) The adversary queries the $\mathcal{O}_{\text{Send}}(\cdot, t_2, \cdot, \cdot)$ oracle for any $t_2 > t$. Moreover, \mathcal{A} can 34
 35 arbitrarily join or leave the group at time t_2 . 35
 36 (4) The adversary correctly guesses the bit b used by the $\mathcal{O}_{\text{Test}}(U, t)$ oracle in an- 36
 37 swering this query. 37
 38

39 The advantage of the adversary \mathcal{A} in attacking the group communication scheme is 39
 40 defined as $\text{Adv}_{\mathcal{A}}(\kappa) = |2 \cdot \text{Pr}[\text{Succ}] - 1|$, where $\text{Pr}[\text{Succ}]$ is the probability that the 40
 41 event **Succ** occurs, and the probability is taken over the coins used by \mathcal{GC} and by \mathcal{A} . 41
 42 We say a scheme is **secure** if for all probabilistic polynomial-time adversary \mathcal{A} it 42
 43 holds that $\text{Adv}_{\mathcal{A}}(\kappa)$ is negligible in κ . 43

1 It is trivial to see that strong-security implies backward-security in the
 2 passive model, and that security implies forward-security in the passive attack
 3 model.

4
 5 3.3. Relationships between the security notions

6 We summarize the relationships between the security notions of stateful group
 7 communication schemes in Fig. 3, where $X \rightarrow Y$ means X is stronger than Y ,
 8 $X \leftrightarrow Y$ means X is equivalent to Y , $X \not\rightarrow Y$ means X does not imply Y , and
 9 $X \stackrel{?}{\not\rightarrow} Y$ means it is unclear where X does not imply Y . Below we elaborate on the
 10 non-trivial relationships showed in Fig. 3.

11 **Proposition 3.1.** *If a stateful group communication scheme is strongly-secure,*
 12 *then it is also secure.*

13 **Proof.** This is almost immediate because, on one hand, the definition of strong-
 14 security ensures the secrecy of $k^{(t)}$ even if \mathcal{A} corrupts some $U \in \Delta^{(t_3)}$ where
 15 $t_3 > t$, and on the other hand, the definition of security ensures the secrecy of
 16 $k^{(t)}$ only if \mathcal{A} does not corrupt any $U \in \Delta^{(t_3)}$ for any $t_3 > t$. \square

17 **Proposition 3.2.** *A stateful group communication scheme that is secure is not nec-*
 18 *essarily strong-secure.*

19 **Proof.** The fact that security does not imply strong-security is implied by
 20 Theorem 5.1, which states that LKH is secure, and that LKH is insecure against
 21 an active outside attacker (cf. the attack scenario in Section 1.1). \square

22 The above proposition implies that for a stateful group communication scheme,
 23 one only needs to show that it is strongly-secure.

24 **Proposition 3.3.** *A stateful group communication scheme is backward-secure in the*
 25 *passive attack model iff it is forward-secure in the passive attack model.*

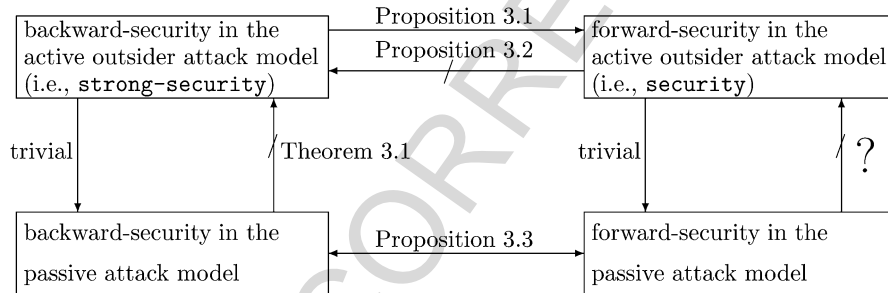


Fig. 3. The relationships between the security notions in stateful group communication schemes.

Proof. First we show that a group communication scheme that is not forward-secure in the passive attack model is also not backward-secure in the passive attack model. Suppose \mathcal{A} first joins the group at time t_1 and then leaves the group at time t_2 where $t_1 < t_2$. Since the scheme is not forward-secure in the passive attack model, \mathcal{A} can distinguish $k^{(t_3)}$ from a random string for some $t_3 > t_2$ with a non-negligible probability. Now suppose \mathcal{A} re-joins the group at time t_4 for some $t_4 > t_3$. Then, with respect to this re-joining event, \mathcal{A} can distinguish $k^{(t_3)}$ from a random string with a non-negligible probability. Since \mathcal{A} did not make any \mathcal{O}_{Reveal} or $\mathcal{O}_{corrupt}$ query, the scheme is not backward-secure in the passive attack model. \square

Now we show that a group communication scheme that is not backward-secure in the passive attack model is also not forward-secure in the passive attack model. Suppose \mathcal{A} first joins the group at time t_1 , leaves the group at time t_2 , and re-joins the group at time t_3 , where $t_1 < t_2 < t_3$. Since the scheme is not backward-secure in the passive attack model, \mathcal{A} can distinguish $k^{(t)}$ from a random string for some $t_2 \leq t < t_3$ with a non-negligible probability. This also means that, with respect to the leaving event at time t_2 , \mathcal{A} can distinguish $k^{(t)}$ from a random string for some $t \geq t_2$ with a non-negligible probability. Since \mathcal{A} does not make any \mathcal{O}_{Reveal} or $\mathcal{O}_{corrupt}$ query, the scheme is not forward-secure in the passive attack model. \square

We do not know whether forward-security in the passive attack mode also implies forward-security in the active outsider attack model. The relationship may seem trivial at a first glance, since all the corrupt members are revoked before the “challenge” session, and the adversary is not allowed to corrupt any member after the “challenge” session. Although it can indeed be shown that the implication holds, provided that the adversary is *static* (meaning that the adversary decides which principals in \mathbb{ID} it will corrupt at system initialization), in the more interesting case that the adversary is *adaptive*, we do not know how to prove it.

Theorem 3.1. *There exists a group communication scheme that is backward-secure in the passive attack model but not strongly-secure (i.e., backward-secure in the active outsider attack model).*

Proof. Theorem 5.1 shows that LKH is secure (i.e., forward-secure in the active outsider attack model), which trivially means that it is also forward-secure in the passive attack model. Then, Proposition 3.3 shows that it is also backward-secure in the passive attack model.

On the other hand, the attack scenario shown in Section 1.1 states that LKH is not backward-secure in the active outsider attack model. \square

4. A compiler for stateful group communication schemes

Suppose $\{f_k\}$ is a secure pseudorandom function family. Now we present a compiler that transforms a secure group communication scheme, $\text{SGC} =$

(Setup, Join, Leave, Rekey), into a strongly-secure one, $\text{SSGC} = (\text{Setup}^*, \text{Join}^*, \text{Leave}^*, \text{Rekey}^*)$. The compiler applies to the subclass of stateful group communication schemes where the different keys belong to $K_{\mathcal{GC}}^{(t)}$ are computationally independent of each other, where $t = 0, 1, 2, \dots$. In what follows “a key k needs to be changed” means that it should be substituted with a random key that is information-theoretically independent of k .

The key idea behind the compiler is to update the keys, which are possibly used to encrypt the new keys that need to be securely sent to the legitimate users, at each join, leave, or rekey event via an appropriate family of pseudorandom functions. As a result, compromise of a current key does not allow the adversary to recover the corresponding past keys.

Setup*: This is the same as SGC.Setup .

Join*: This algorithm is executed by \mathcal{GC} at time, say, t . Let K be the set of keys that need to be changed (including the group key $k^{(t-1)}$), K^* be the set of common key(s) shared between the \mathcal{GC} and the joining user(s), and K^{**} be the new keys (including the new group key $k^{(t)}$) that are used to replace the keys in K .

1. Execute SGC.Join except for the following: (1) for every $k_i \in (K_{\mathcal{GC}}^{(t-1)} \setminus \{k^{(t-1)}\}) \cup K^*$, let $f_{k_i}(0)$ play the role of k_i in SGC.Join ; (2) for every $k_i \in K^{**} \setminus \{k^{(t)}\}$ that is used as an encryption key in SGC.Join , let $f_{k_i}(0)$ play the role of k_i .
2. Every individual key $k_i \in (K_{\mathcal{GC}}^{(t-1)} \setminus K) \cup K^* \cup (K^{**} \setminus \{k^{(t)}\})$ is replaced by $f_{k_i}(1)$.

Leave*: This algorithm is executed by \mathcal{GC} at time, say, t . Let K be the set of keys that need to be changed (including the group key $k^{(t-1)}$) or eliminated, and K^{**} be the new keys (including the new group key $k^{(t)}$) that are used to replace (possibly a subset of) the keys in K .

1. Execute SGC.Leave except for the following: (1) for every $k_i \in K_{\mathcal{GC}}^{(t-1)} \setminus K$, let $f_{k_i}(0)$ play the role of k_i in SGC.Leave ; (2) for every $k_i \in K^{**} \setminus \{k^{(t)}\}$ that is used as an encryption key in SGC.Leave , let $f_{k_i}(0)$ play the role of k_i .
2. Every individual key $k_i \in (K_{\mathcal{GC}}^{(t-1)} \setminus K) \cup (K^{**} \setminus \{k^{(t)}\})$ is replaced by $f_{k_i}(1)$.

Rekey*: There are two cases.

- The rekeying event is incurred by a **Leave** event at time t . In this case, every honest leaving user should erase all the secrets as in SGC.Rekey , and every remaining user, $V \in \Delta^{(t)}$, executes the following. Denote by $K'_V \subseteq K_V^{(t-1)}$ the subset of keys that need to be changed to a set of new keys K''_V . (We notice that both K'_V and K''_V can be derived by V after receiving the rekeying message and that $k^{(t)} \in K''_V$.) First, V executes

1 **SGC.Rekey** except for letting $f_{k_i}(0)$ play the role of k_i under the circum- 1
 2 stance that $k_i \in K_V^{(t-1)} \setminus \{k^{(t-1)}\}$ or $k_i \in K_V'' \setminus \{k^{(t)}\}$ is used as an encryp- 2
 3 tion key, and updates every $k_i \in (K_V^{(t-1)} \setminus K_V') \cup (K_V'' \setminus \{k^{(t)}\})$ as $f_{k_i}(1)$. 3
 4 Second, V erases the outdated keys (except $K_V^{(t)}$) as in **SGC.Rekey**. 4
 5

- 6 • The rekeying event is incurred by a **Join** event at time t . We notice that 6
 7 user $V \in \Delta^{(t)}$ holds a set of keys $K_V^{(t-1)}$ (in the case of V being a join- 7
 8 ing user, $K_V^{(t-1)}$ consists of the only common key between \mathcal{GC} and V), of 8
 9 which a subset K_V' of keys (which may be empty) are to be changed to a 9
 10 set of new keys K_V'' . (We notice that both K_V' and K_V'' can be derived by 10
 11 V after receiving the rekeying message and that $k^{(t)} \in K_V''$.) First, V ex- 11
 12 ecutes **SGC.Rekey** except for letting $f_{k_i}(0)$ play the role of k_i under the 12
 13 circumstance that $k_i \in K_V^{(t-1)} \setminus \{k^{(t-1)}\}$ or $k_i \in K_V'' \setminus \{k^{(t)}\}$ is used as 13
 14 an encryption key, and updates every $k_i \in (K_V^{(t-1)} \setminus K_V') \cup (K_V'' \setminus \{k^{(t)}\})$ 14
 15 as $f_{k_i}(1)$. Second, $V \in \Delta^{(t)}$ erases the outdated keys (other than $K_V^{(t)}$) as 15
 16 in **SGC.Rekey**. 16
 17

18 4.1. Analysis 18

19 First we analyze the complexity of **SSGC**. 19

- 20 • It does not introduce any extra communication complexity over **SGC**; this is 20
 21 important in many applications such as MANETs and sensor networks. (In Sec- 21
 22 tion 4.2 we further reduce the communication complexity.) 22
- 23 • It does not introduce any extra storage complexity over **SGC**, provided that the 23
 24 temporary storage for the keys such as $f_{k_i}(0)$ is insignificant. This is at least 24
 25 true for most applications including MANETs and sensor networks. 25
- 26 • The only extra complexity of **SSGC** over **SGC** is the evaluation of the pseudo- 26
 27 random functions. Specifically, the server needs to conduct $O(\max\{|K_{\mathcal{GC}}^{(t-1)}|,$ 27
 28 $|K_{\mathcal{GC}}^{(t)}|\})$ pseudorandom function evaluation operations; a user V needs to con- 28
 29 duct $O(\max\{|K_U^{(t-1)}|, |K_U^{(t)}|\})$ pseudorandom function operations. We notice 29
 30 that typically $|K_U^{(t)}| = O(\log(|K_{\mathcal{GC}}^{(t)}|))$ (e.g., [28]). This should be insignificant 30
 31 for most applications including MANETs and sensor networks. 31
 32

33 Now we prove that **SSGC** is indeed strongly-secure. The intuition that 33
 34 **SSGC** is strongly-secure (and thus defeats the attacks presented in the Intro- 34
 35 duction) is due to the following fact: compromise of all of the current keys held by a 35
 36 user does not necessarily allow the adversary to recover any of the past keys, which 36
 37 may have been used to secure the transmission of other keys. 37
 38

39 **Theorem 4.1.** Assume $\{f_k\}$ is a secure pseudorandom function family (as specified 39
 40 in Section 2). If **SGC** is secure, then **SSGC** is strongly-secure. 40
 41

42 43

Proof (sketch). We show that if **SSGC** is not strongly-secure, then **SGC** is not secure. Note that the key difference between the two security notions is whether the adversary is allowed to corrupt a legitimate user after the rekeying event of interest. Note also that after a rekeying event in **SSGC** all the new keys are either information-theoretically or computationally independent of each other.

First, consider a mental scheme that is the same as in **SSGC** except that the keys of the form $f_{k_i}(0)$ are always substituted with freshly and independently chosen random keys, where k_i is not held by any corrupt user. We claim that this mental scheme achieves strong-security; otherwise, there is an efficient algorithm to break the security of **SGC**. To see this, we construct a simulator that has access to a challenge **SGC** environment. Since the number of rekeying events in **SSGC** is polynomially-bounded, the simulator has an inverse polynomial probability in successfully guessing the rekeying event of interest – the event corresponding to the $\mathcal{O}_{Test}(\cdot, \cdot)$ query.

1. The simulator interacts with the adversary as in **SSGC**; this can be done because the simulator has complete control over the keys utilized in the **SSGC**. We notice that the simulator can answer any queries, including \mathcal{O}_{reveal} and $\mathcal{O}_{corrupt}$.
2. When the simulated **SSGC** execution reaches the point of interest, the simulator asks the challenge **SGC** environment to establish an instance of **SGC** with the same set of users. The establishment of the instance is based on the rekeying event incurred by the adversary in **SSGC**, so that the legitimate users hold the corresponding keys as in **SGC.Setup**. This substitution can get through because the definition of strong-security ensures that the adversary in **SSGC** does not corrupt any legitimate user during the rekeying event.
3. At the next rekeying event, the simulator can continue its execution of the **SSGC** because it can utilize independent secrets that are freshly chosen by itself. We notice that the simulator can answer any queries, including \mathcal{O}_{reveal} and $\mathcal{O}_{corrupt}$, as it can simulate the **SSGC** environment in any future rekeying events.

Second, it is clear that the difference between **SSGC** and the aforementioned mental scheme is that the keys utilized in the rekeying events are either series of keys in the forms of $f_{k_i}(1)$ where the k_i 's are secret from the adversary, or freshly and independently chosen at random. We claim that the two cases are indistinguishable as long as the pseudorandom function family is secure. To see this, we notice that no adversary can, with a non-negligible probability, distinguish a single key-chain of a fixed key identity, namely $f_{k_i}(1), f_{f_{k_i}(1)}(1), f_{f_{f_{k_i}(1)}(1)}(1), \dots$ where k_i is secret from the adversary, from a sequence of random secrets. Otherwise, we can construct an algorithm to distinguish a pseudorandom function from a random one with a non-negligible probability (because the number of rekeying events is polynomially-bounded). Conditioned on the fact that the number of keys is polynomially-bounded,

1 we conclude that the keys derived from pseudorandom functions are indistinguishable from the keys that are freshly and independently chosen; otherwise, a standard
 2 hybrid argument shows that there exists an algorithm that is able to distinguish a
 3 pseudorandom function from a random one (because there are at most a polynomial
 4 number of key chains). \square

6 4.2. Performance optimization

8 In this section we show how to reduce the communication complexity in
 9 the SSGC; this might be very useful in applications such as MANETs and sensor
 10 networks. Suppose a Join event occurs at time t . The key observation includes:
 11

- 12 1. In Join* of SSGC we could simply let the server sends the updated keys to
 13 the joining user U . We notice that, before U receiving the rekeying message
 14 from the server, $K_U^{(t-1)}$ consists of a single key, denoted by k^* , that is also
 15 known to the server. After sending the rekeying message, the server update
 16 $K_{GC}^{(t-1)} = \{k_i\}$ to $K_{GC}^{(t)} = \{f_{k_i}(1)\} \cup \{f_{k^*}(1)\}$.
- 17 2. When the joining user U executes Rekey* corresponding to the Join* (i.e.,
 18 after receiving the rekeying message), it lets $f_{k^*}(0)$ plays the role of k^* . Then,
 19 U updates k^* to $f_{k^*}(1)$ while keeping intact the other keys received from the
 20 server.
- 21 3. When an existing user $V \in \Delta^{(t-1)}$ executes Rekey* corresponding to
 22 the Join*, it simply updates every $k_i \in K_V^{(t-1)}$ (including the group key)
 23 to $f_{k_i}(1)$.
- 24 4. The encryption of group communications is based on new group key $k^{(t)} =$
 25 $f_{k^{(t-1)}}(1)$.

26 We notice that the idea of substituting k_i via a certain function was pointed out
 27 in [8,26] with respect to the specific scheme of [28]. Here we show that it can actually
 28 be extended to accommodate the class of group communication schemes discussed
 29 in this paper. This justifies why we treat it as a possible feature of the compiler, which
 30 we call the *optimized compiler*.
 31

32 **Theorem 4.2.** Assume $\{f_k\}$ is a secure pseudorandom function family, and SGC is
 33 secure. If SGC does not adopt the afore-discussed performance optimization (oth-
 34 erwise, the optimized compiler does not gain anything over the original compiler),
 35 then the scheme output by the optimized compiler is also strongly-secure.
 36

37 The proof is similar to the proof of Theorem 4.1, and thus omitted.
 38

40 5. A concrete Strongly-Secure stateful group communication scheme

41 In the last section we presented a compiler that can transform a certain se-
 42 cure stateful group communication scheme into a strongly-secure one. In
 43

1 this section we present a concrete `strongly-secure` stateful group communica- 1
 2 tion scheme, which is obtained by applying the compiler to LKH [28] that is shown 2
 3 to be `secure` in Section 5.3. First we briefly review LKH. 3
 4

5 5.1. The model of LKH 5

6
 7 The model of LKH is best known as a *key tree*, which outperforms the others 7
 8 (e.g., star key graph, or general key graph which actually leads to a certain NP-hard 8
 9 problem as we always need to minimize the communication complexity). A key tree 9
 10 T can be seen as a special class of directed acyclic graph with two types of nodes: 10
 11 *u-nodes* representing users and *k-nodes* representing keys. Each *u-node* is a leaf that 11
 12 has one outgoing edge but no incoming edge, and each *k-node* is an inner node that 12
 13 has one or more incoming edges. Moreover, there is a *k-node* (i.e., the root) that 13
 14 has incoming edges but no outgoing edge. In other words, the edges go from leaves 14
 15 towards the root. 15

16 Let U be a finite and nonempty set of users and K be a finite and nonempty set of 16
 17 keys. We are interested in a relation, $R \subseteq U \times K$, that can be specified by a key tree 17
 18 T as follows: 18

- 19 • There is a one-to-one correspondence between U and the set of *u-nodes* in T . 19
- 20 • There is a one-to-one correspondence between K and the set of *k-nodes* in T . 20
- 21 • $(u, k) \in R$ if and only if there is a directed path in T from the *u-node* that 21
 22 corresponds to a user $u \in U$ to the *k-node* that corresponds to a key $k \in K$. 22

23
 24 This means that the group key is at the root of the tree, which is shared by all the 24
 25 users in U . Since a key tree can be specified by two parameters – the height h of the 25
 26 tree is the length (in number of edges) of the longest directed path in the tree, and 26
 27 the degree d of the tree is the maximum number of incoming edges of a node in the 27
 28 tree – each user in U has at most h keys. 28

29 In order to clarify the presentation, we define two functions, $\text{KEYSET} : U \rightarrow K$ 29
 30 and $\text{USERSET} : K \rightarrow U$, as follows: 30

$$31 \quad \text{KEYSET}(u) = \{k \mid (u, k) \in R\}, \quad 31$$

$$32 \quad \text{USERSET}(k) = \{u \mid (u, k) \in R\}. \quad 32$$

33
 34 Intuitively, $\text{KEYSET}(u)$ is the set of keys held by user $u \in U$, and $\text{USERSET}(k)$ 35
 36 is the set of users that hold key $k \in K$. Moreover, it is natural to generalize the 36
 37 definitions of $\text{KEYSET}(u \in U)$ to $\text{KEYSET}(U' \subseteq U) = \bigcup_{u \in U'} \text{KEYSET}(u)$, and of 37
 38 $\text{USERSET}(k \in K)$ to $\text{USERSET}(K' \subseteq K) = \bigcup_{k \in K'} \text{USERSET}(k)$. 38
 39

40 5.2. A Strongly-Secure stateful group communication scheme 40

41
 42 The new scheme is obtained by applying the compiler described in Section 4 to 42
 43 LKH based on the so-called *group-oriented* rekeying strategy, which is reviewed in 43

Appendix A for completeness. (LKH can be based on the less efficient *key-oriented* and *user-oriented* strategies [28]. Nevertheless, it should be straightforward to adapt our scheme to these rekeying strategies.) The scheme consists of four protocols, namely $\text{SSGC} = (\text{Setup}^*, \text{Join}^*, \text{Leave}^*, \text{Rekey}^*)$.

Setup*: The key server generates a key k_i for each k -node. After the initialization, each user (corresponding to a u -node) holds the keys corresponding to the path from its parent k -node to the root.

For example, if the initial system configuration is like in Fig. 1(a), then user u_5 holds keys, k_5, k_{456}, k_{1-8} , where k_{1-8} is the group key.

Join*: After granting a join request from user u , the key server s creates a new u -node for user u and a new k -node for its individual key k_u . Then, server s finds an existing k -node (called the *joining point* for this join request) in the key tree and attaches the k -node k_u to the joining point as its child. As a consequence, the keys corresponding to the path – starting at the joining point and ending at the root – need to be changed. The algorithm is specified in Fig. 4, whose basic idea can be summarized as follows:

1. For each k -node x whose key needs to be changed, say, from \bar{k}_i to freshly chosen \hat{k}_i , the server constructs two rekeying messages. The first rekeying message is the encryption of new key \hat{k}_i with $f_{\bar{k}_i}(0)$, where \bar{k}_i is a non-root key that needs to be changed, and is sent to $\text{USERSET}(\bar{k}_i)$, namely the set of users that share \bar{k}_i . The second rekeying message contains the encryption of the new key \hat{k}_i with the individual key of the joining user, and is sent to the joining user. Moreover, these rekeying messages are appropriately grouped together.

Join protocol for group-oriented rekeying: // suppose user u joins the group

server s generates a new key k_u for user u

server s finds a joining point x_j

server s attaches k_u to x_j

let x_0 be the root

denote by x_{i-1} the parent of x_i for $1 \leq i \leq j$

$\bar{k}_{j+1} \leftarrow k_u$

let $\bar{k}_0, \bar{k}_1, \dots, \bar{k}_j$ be the current keys of x_0, \dots, x_j , respectively

server s generates fresh keys $\hat{k}_0, \hat{k}_1, \dots, \hat{k}_j$ // new keys of x_0, \dots, x_j

$s \rightarrow \text{USERSET}(\bar{k}_0) : \{\hat{k}_0\}_{\bar{k}_0}, \{\hat{k}_1\}_{f_{\bar{k}_1}(0)}, \dots, \{\hat{k}_j\}_{f_{\bar{k}_j}(0)}$

$s \rightarrow \{u\} : \{\hat{k}_0, \hat{k}_1, \dots, \hat{k}_j\}_{f_{\bar{k}_{j+1}}(0)}$

FOR all $\bar{k} \in (\text{KEYSET}(\text{USERSET}(\bar{k}_0)) \setminus \{\bar{k}_0, \bar{k}_1, \dots, \bar{k}_j\}) \cup \{\bar{k}_{j+1}\}$

$\cup \{\hat{k}_1, \dots, \hat{k}_j\}$

$\bar{k} \leftarrow f_{\bar{k}}(1)$

Fig. 4. Join-incurred group-oriented rekeying.

2. Any other key \bar{k}_j that needs not to be changed is replaced by $f_{\bar{k}_j}(1)$.

For example, if u_9 joins the group configured as in Fig. 1(a), then u_9 is granted to join at joining point of k -node k_{78} . Then, the group key is changed from k_{1-8} to k_{1-9} , and k_{78} is replaced with a new k_{789} . The rekeying messages sent to the users are:

$$\begin{aligned} s \rightarrow \{u_1, \dots, u_8\} &: \{k_{1-9}\}_{k_{1-8}}, \{k_{789}\}_{f_{k_{78}}(0)}, \\ s \rightarrow \{u_9\} &: \{k_{1-9}, k_{789}\}_{f_{k_9}(0)}. \end{aligned}$$

Finally, k_i is substituted with $f_{k_i}(1)$ for $i \in \{1, 2, 3, 4, 5, 6, 7, 8, 9, 123, 456, 789\}$. The attack presented in the Introduction is blocked because, for example, compromise of $f_{k_9}(1)$ does not lead to the exposure of $f_{k_9}(0)$, where k_9 is not known to the adversary (because it has been securely erased). As a result, the past group key k_{1-9} cannot be recovered by the adversary.

Leave*: After granting a leave request from user u , the key server s updates the key tree by deleting the u -node for user u and the k -node for its individual key from the key tree. The parent of the k -node corresponding to the user's individual key is called the *leaving point*. As a consequence, the keys corresponding to the path – starting at the leaving point and ending at the root – need to be changed. The algorithm is specified in Fig. 5, whose basic idea can be summarized as follows:

1. For each k -node x whose key needs to be changed, say, from \bar{k}_i to freshly chosen \hat{k}_i , the server constructs a rekeying message that is the encryption of \hat{k}_i with the keys of x 's children in the new key tree. Note that “the keys of x 's children in the new key tree” are either certain new keys that need to be distributed, or some current keys that need not to be changed (although they will be appropriately updated).
2. Any other key \bar{k}_j that needs not to be changed is replaced by $f_{\bar{k}_j}(1)$.

For example, if u_8 leave the group as configured in Fig. 1(b), the leaving point is the k -node k_{789} . Then, the group key is changed from k_{1-9} to $k_{1-7,9}$, and the key of leaving point is changed from k_{789} to $k_{7,9}$ in Fig. 1(c). The rekeying message sent to the users is:

$$\begin{aligned} s \rightarrow \{u_1, \dots, u_7, u_9\} &: \{k_{1-7,9}\}_{f_{k_{123}}(0)}, \{k_{1-7,9}\}_{f_{k_{456}}(0)}, \{k_{1-7,9}\}_{f_{k_{7,9}}(0)}, \\ &\{k_{7,9}\}_{f_{k_7}(0)}, \{k_{7,9}\}_{f_{k_9}(0)}. \end{aligned}$$

Finally, k_i is updated to $f_{k_i}(1)$ for $i \in \{1, 2, 3, 4, 5, 6, 7, 9, 123, 456\}$, and $k_{7,9}$ is updated to $f_{k_{7,9}}(1)$. The attack presented in the Introduction is blocked because, for example, compromise of $f_{k_9}(1)$ does not lead to the exposure of $f_{k_9}(0)$, where k_9 is not known to the adversary (because it has been securely erased). As a result, $k_{7,9}$, and thus the past group key $k_{1-7,9}$ cannot be recovered by the adversary.

1	Leave protocol for group-oriented rekeying: // suppose u leaves the group	1
2	let x_{j+1} be the deleted k -node for k_u	2
3	$\bar{k}_{j+1} \leftarrow k_u$	3
4	server s finds the leaving point x_j (parent of k_u)	4
5	server s removes \bar{k}_{j+1} from the key tree	5
6	let x_0 be the root	6
7	denote by x_{i-1} the parent of x_i where $1 \leq i \leq j$	7
8	let k_0, k_1, \dots, k_j be the keys of x_0, x_1, \dots, x_j // they need to be changed	8
9	server s generates fresh keys $\hat{k}_0, \hat{k}_1, \dots, \hat{k}_j$ as the new keys of x_0, x_1, \dots, x_j	9
10	FOR $i = 0$ TO $j - 1$	10
11	let $\bar{k}_{i_1}, \dots, \bar{k}_{i_{z_i}}$ be the keys at the children of x_i in the new key tree	11
12	where \bar{k}_{i_a} is to be changed to \hat{k}_{i+1} for some $a \in \{1, \dots, z_i\}$	12
13	$L_i \leftarrow (\{\hat{k}_i\}_{f_{\bar{k}_{i_1}}(0)}, \dots, \{\hat{k}_i\}_{f_{\bar{k}_{i_{a-1}}}(0)}, \{\hat{k}_i\}_{f_{\bar{k}_{i+1}}(0)},$	13
14	$\{\hat{k}_i\}_{f_{\bar{k}_{i_{a+1}}}(0)}, \dots, \{\hat{k}_i\}_{f_{\bar{k}_{i_{z_i}}}(0)})$	14
15	let $\bar{k}_{j_1}, \dots, \bar{k}_{j_{z_j}}$ be the keys at the children of x_j in the new key tree	15
16	$L_j \leftarrow (\{\hat{k}_j\}_{f_{\bar{k}_{j_1}}(0)}, \dots, \{\hat{k}_j\}_{f_{\bar{k}_{j_{z_j}}}(0)})$	16
17	$s \rightarrow \text{USERSET}(\bar{k}_0) \setminus \{u\} : (L_0, \dots, L_j)$	17
18	FOR all $\bar{k} \in (\text{KEYSET}(\text{USERSET}(\bar{k}_0)) \setminus \{\bar{k}_0, \bar{k}_1, \dots, \bar{k}_{j+1}\}) \cup \{\hat{k}_1, \dots, \hat{k}_j\}$	18
19	$\bar{k} \leftarrow f_{\bar{k}}(1)$	19
20		20
21		21
22		22
23		23
24		24
25		25
26		26
27		27
28		28
29		29
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34		34
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37		37
38		38
39		39
40		40
41		41
42		42
43		43

Fig. 5. Leave-incurred group-oriented rekeying.

Rekey*: If the rekeying event is incurred by a join event, a legitimate user (i.e., an existing one or a joining one) obtains a subset Θ' of $\Theta = \{\hat{k}_0, \hat{k}_1, \dots, \hat{k}_j\}$, and updates each $\hat{k} \in \Theta' \setminus \{\hat{k}_0\}$ to $f_{\hat{k}}(1)$. If the rekeying event is incurred by a leave event, a legitimate user (i.e., one remaining in the group) obtains a subset Θ' of $\Theta = \{\hat{k}_0, \hat{k}_1, \dots, \hat{k}_j\}$, and updates each $\hat{k} \in \Theta' \setminus \{\hat{k}_0\}$ to $f_{\hat{k}}(1)$. In any case, a legitimate user u updates each $k_i \in \text{KEYSET}(u)$ to $f_{k_i}(1)$, as long as k_i is not changed to any key belonging to Θ , and erases the outdated keys. For example, corresponding to the event that u_9 joins the group as shown in Fig. 1(a), u_1 obtains k_{1-9} , updates k_{123} to $f_{k_{123}}(1)$, and updates k_1 to $f_{k_1}(1)$. Whereas, u_9 obtains k_{1-9} as well as k_{789} , updates k_{789} to $f_{k_{789}}(1)$, and updates k_9 to $f_{k_9}(1)$. Corresponding to the event that u_8 leaves the group as shown in Fig. 1(b), u_1 obtains $k_{1-7,9}$, updates k_{123} to $f_{k_{123}}(1)$, and updates k_1 to $f_{k_1}(1)$. Whereas, u_9 obtains $k_{1-7,9}$ as well as $k_{7,9}$, updates $k_{7,9}$ to $f_{k_{7,9}}(1)$, and updates k_9 to $f_{k_9}(1)$.

5.3. Analysis

Theorem 5.1. Assume that the stand-alone encryptions utilized in LKH are based on a secure pseudorandom function family. Then, LKH is secure.

Proof (sketch). Consider a mental scheme that is the same as LKH, except that the encryptions corresponding to the rekeying event of interest – the event corresponding to the $\mathcal{O}_{Test}(\cdot, \cdot)$ query – are based on random functions. This substitution can get through because the definition of *security* requires that there are no corrupt users. We claim that this mental scheme is *secure*; otherwise, a standard hybrid argument shows that the pseudorandom function family is broken because the number of encryptions is polynomially-bounded (which is further based on the fact that the size of the key-tree is polynomially-bounded). Conditioned on the fact that there are a polynomially-bounded number of rekeying events, we conclude that LKH is *secure*. \square

As a corollary of Theorem 4.1 (which states that the compiler transforms a *secure* stateful group communication scheme to a *strongly-secure* one) and Theorem 5.1 (which states that LKH is indeed *secure*), we have:

Corollary 5.1. *The scheme presented in Section 5.2 is strongly-secure.*

5.4. Performance optimization

The improved scheme differs from SSGC only in **Join*** and **Rekey***.

Improved Join*: This algorithm is specified in Fig. 6. It is the same as the **Join*** except the following: (1) instead of freshly choosing new keys for the k -nodes on the path starting at a joining point and ending at the root, we simply update every existing key k as $f_k(1)$, and (2) the new group key for encrypting actual group communications is $f_k(0)$, where k is the already updated key at the root.

Improved Rekey*: It is the same as **Rekey*** except that when the rekeying is incurred by a join event: every existing user v holding a key set $\text{KEYSET}(v)$ needs to

<pre> Join protocol for group-oriented rekeying: // suppose user u joins the group server s generates a new key k_u for user u server s finds a joining point x_j server s attaches k_u to x_j let x_0 be the root denote by x_{i-1} the parent of x_i for $1 \leq i \leq j$ let $\bar{k}_0, \bar{k}_1, \dots, \bar{k}_j$ be the current keys of x_0, \dots, x_j, respectively $\bar{k}_{j+1} \leftarrow k_u$ $s \rightarrow \text{USERSET}(\bar{k}_0)$: "key update" $s \rightarrow \{u\} : \{f_{\bar{k}_0}(1), f_{\bar{k}_1}(1), \dots, f_{\bar{k}_j}(1)\} f_{\bar{k}_{j+1}}(0)$ FOR all $\bar{k} \in \text{KEYSET}(\text{USERSET}(\bar{k}_0)) \cup \{\bar{k}_{j+1}\}$ $\bar{k} \leftarrow f_{\bar{k}}(1)$ </pre>
--

Fig. 6. Improved join-incurred group-oriented rekeying.

1 update every $k \in \text{KEYSET}(v)$ to $f_k(1)$, whereas the joining user u only needs to
 2 update its common key k_u , which is established during the out-of-band approval of
 3 the join request, to $f_{k_u}(1)$. Note that the new group key for encrypting actual group
 4 communications is $f_k(0)$, where k is the already updated key at the root.

5
 6 For example, if u_9 joins the group configured as in Fig. 1(a), then u_9 is granted to
 7 join at the joining point of k -node k_{78} . The key at the root is updated from k_{1-8} to
 8 $k_{1-9} = f_{k_{1-8}}(1)$ such that the new key for encrypting actual group communications
 9 is $f_{k_{1-9}}(0)$, and k_{78} is updated to $k_{789} = f_{k_{78}}(1)$. The sever sends the following
 10 messages:

$$\begin{aligned} 11 \quad s &\rightarrow \{u_1, \dots, u_8\} : \text{"key update"} \\ 12 \quad s &\rightarrow \{u_9\} : \{k_{1-9}, k_{789}\}_{f_{k_9}(0)}. \end{aligned}$$

13
 14
 15 Every existing user u_i , $i \in \{1, 2, 3, 4, 5, 6, 7, 8\}$, with key set K_i , updates every
 16 $k \in K_i$ as $f_k(1)$. For example, u_7 updates k_{1-8} to $k_{1-9} = f_{k_{1-8}}(1)$, updates k_{78} to
 17 $k_{789} = f_{k_{78}}(1)$, and updates k_7 to $k_7 = f_{k_7}(1)$. On the other hand, the joining user u_9
 18 only needs to update k_9 to $k_9 = f_{k_9}(1)$, which means that it keeps $(k_{1-9}, k_{89}, k_9 =$
 19 $f_{k_9}(1))$.

20
 21 As a corollary of Theorem 4.2 (which states that the optimized compiler in
 22 Section 4.2 transforms a secure stateful group communication scheme into a
 23 strongly-secure one) and Theorem 5.1 (which states that LKH is indeed se-
 24 cure), we have

25
 26 **Corollary 5.2.** *The optimized scheme in Section 5.4 is strongly-secure.*

27 28 29 30 6. The case of stateless group communication schemes

31
 32 Recall that we briefly reviewed the subset-cover framework [22] in Section 1.1.
 33 This section is organized as follows. In Section 6.1 we discuss the models and se-
 34 curity definitions, including the notions of strong-security (i.e., backward-
 35 security in the active outsider attack model) and of security (i.e., forward-
 36 security in the passive attack model). In Section 6.2 we explore the relationships be-
 37 tween the security notions. In Section 6.3 we present a compiler that can transform
 38 a subclass of secure stateless group communication schemes into strongly-
 39 secure ones, whose security is analyzed in Section 6.4. A concrete strongly-
 40 secure stateless group communication scheme, which is based on the *complete*
 41 *subtree method* [22], is presented in Section 6.5. Some practical issues are discussed
 42 in Section 6.6.

6.1. Model and security of stateless group communication schemes

The subset-cover framework of [22] was briefly reviewed in Fig. 2. More specifically, let κ be a security parameter, \mathcal{N} be the set of all users such that $|\mathcal{N}| = N$ is polynomially-bounded, and $\mathcal{R} \subset \mathcal{N}$ be a group of $|\mathcal{R}| = r$ users whose decryption privileges should be revoked. Let E_L be a symmetric key cryptosystem secure against an adaptive chosen-plaintext attack, and F_K be a symmetric key cryptosystem with a weaker security property called indistinguishability under a single chosen-plaintext attack in [22] (which is called “IND-P0-C0 security” in [13]).³

Recall that the goal of a stateless group communication scheme is to allow a center (or group controller, server, or sender) to transmit a message M to all users such that any user $u \in \mathcal{N} \setminus \mathcal{R}$ can decrypt the message correctly, while even a coalition consisting of all members of \mathcal{R} cannot decrypt it. Suppose S_1, \dots, S_w are a collection of subsets of users, where $S_j \subseteq \mathcal{N}$ for $1 \leq j \leq w$, and each S_j is assigned a long-lived key L_j such that each $u \in S_j$ should be able to deduce L_j from its secret information I_u . Given a revoked set \mathcal{R} , if one can partition $\mathcal{N} \setminus \mathcal{R}$ into (ideally disjoint) sets S_{i_1}, \dots, S_{i_m} such that $\mathcal{N} \setminus \mathcal{R} \subseteq \cup_{\ell=1}^m S_{i_\ell}$, then a message-encryption key K can be encrypted m times with L_{i_1}, \dots, L_{i_m} , and each user $u \in \mathcal{N} \setminus \mathcal{R}$ can obtain K and thus M .

In what follows, by “ \mathcal{A} corrupts a user u ” we mean that not only the internal state of u (including I_u) is given to \mathcal{A} , but also u will behave under \mathcal{A} ’s control (i.e., Byzantine); by “ u is revoked” we mean that u is not entitled to receive the message with respect to the specified session(s). For simplicity, we assume that a user, once corrupted, is always corrupt.

Stateless group communication schemes are indeed simpler than stateful ones because (1) both the joining and leaving operations are implicit – the rekeying messages may even be coupled with the payload, and (2) when a user (re-)joins a group, its long-term keys can indeed be reused. Therefore, the model of stateless group communication schemes can also be correspondingly simplified. In particular, we assume the center keeps an incremental counter for each broadcast messages so that encryptions may be simply denoted by $C^{(1)}, C^{(2)}, \dots$ and the corresponding plaintext messages may be denoted by $M^{(1)}, M^{(2)}, \dots$. One may think each $C^{(i)}$ corresponds to an “rekeying” event with revocation set $\mathcal{R}^{(i)}$ for $i = 1, 2, \dots$. Note that $\mathcal{R}^{(i)} \neq \mathcal{R}^{(i+1)}$.

³Notice that [22] required that E_L be secure against chosen-ciphertext attacks, whereas we require it to be secure against chosen-plaintext attacks. The reason is that we need to we assume that the underlying communication channels are authenticated. While this naturally prevents chosen-ciphertext attacks, it also avoid another subtle attack, namely that a dishonest user could successfully cheat an honest user into accepting an impersonating message. The reason is simply due to the fact that E_L being secure against chosen-ciphertext attacks does not necessarily prevent this attack, because the dishonest user also knows the common secret key. This subtlety is well understood in the context of group communications (cf. [5]).

1 We assume that during the system initialization the center can communicate with 1
 2 each legitimate user through an *authenticated private* channel. In practice, the 2
 3 authenticated private channel can be implemented by a two-party authenticated key- 3
 4 exchange protocol, which should also ensure, as in the case of stateful group 4
 5 communication schemes, that certain relevant keys are securely erased after the initial- 5
 6 ization. Further, we assume that after the system initialization the center can com- 6
 7 municate with a user through an *authenticated* channel. 7

8 In parallel to the case of stateful group communication schemes, we define two 8
 9 adversarial models for stateless group communication schemes: the *active outsider* 9
 10 *attack model* and the *passive outsider attack model*. 10

11 **Definition 6.1** (active outsider attack model). With respect to a given i th broadcast 11
 12 message $C^{(i)}$, we say a user u is legitimate if $u \in \mathcal{N} \setminus \mathcal{R}^{(i)}$, and is illegitimate (or 12
 13 an outsider) otherwise. By “active outsider attack model” we mean the adversarial 13
 14 model in which an outsider \mathcal{A} of the i th broadcast message, which may be called 14
 15 the “challenge” message, is allowed to corrupt legitimate users of $C^{(j)}$ for any $j > i$ 15
 16 (i.e., $u \in \mathcal{N} \setminus \mathcal{R}^{(j)}$). 16

17 **Definition 6.2** (passive attack model). In this adversarial model, the adversary \mathcal{A} is 17
 18 not allowed to corrupt any other legitimate member. In other words, the adversary 18
 19 is only allowed to decide when it is to be revoked (though in an arbitrary fashion). 19
 20 Formally, \mathcal{A} cannot corrupt any $u \in \mathcal{N} \setminus \{\mathcal{A}\}$ for $i = 1, 2, \dots$ 20
 21 21

22 In each of the two models, we define two security notions: backward-security 22
 23 and forward-security. That is, we have four security notions: (1) forward-security 23
 24 in the active outsider attack model or simply *security* for short, (2) backward- 24
 25 security in the active outsider attack model or simply *strong-security* for 25
 26 short, (3) forward-security in the passive attack model, and (4) backward-security 26
 27 in the passive attack model. 27
 28 28

29 **Definition 6.3** (*security*; adapted from [22]). Consider an adversary \mathcal{A} that gets 29
 30 to 30

- 31 1. Select adaptively $\mathcal{R}^{(1)}, \mathcal{R}^{(2)}, \dots, \mathcal{R}^{(\ell_1)}$ of receivers, obtain I_u for all $u \in \mathcal{R}^{(i)}$ 31
 32 and see $C^{(1)}, C^{(2)}, \dots, C^{(\ell_1)}$ for $i = 1, 2, \dots, \ell_1$. 32
 33 33
- 34 2. Choose a message M as the challenge plaintext and a set \mathcal{R} of revoked 34
 35 users that must include all the ones it corrupted (but may contain more); i.e., 35
 36 $\cup_{i=1}^{\ell_1} \mathcal{R}^{(i)} \subseteq \mathcal{R}$. \mathcal{A} then receives an encrypted message C with a revoked set \mathcal{R} , 36
 37 where C is the encryption of either M or a random message of the same length. 37
 38 We may call this the “challenge” message. 38
 39 39
- 40 3. For $i = \ell_1 + 2, \ell_1 + 3, \dots$, the following restrictions apply. (1) Even if $\mathcal{A} \in \mathcal{N}$, 40
 41 \mathcal{A} can only decide whether $\mathcal{A} \in \mathcal{R}^{(i)}$. (2) Even if $\mathcal{R}^{(i)} \setminus \{\mathcal{A}\} \neq \emptyset$, \mathcal{A} has no 41
 42 access to any I_u for $u \in \mathcal{R}^{(i)} \setminus \{\mathcal{A}\}$. 42
 43 43

Now \mathcal{A} has to guess whether C corresponds to the encryption of the real message M or a random message. Denote by **Succ** the event that \mathcal{A} makes the right guess. The advantage of \mathcal{A} is defined as $\text{Adv}_{\mathcal{A}}(\kappa) = |2 \cdot \Pr[\text{Succ}] - 1|$, where $\Pr[\text{Succ}]$ is the probability that the event **Succ** occurs, and the probability is taken over the coins used by the center and by \mathcal{A} . We say that a stateless group communication scheme is *secure* (or forward-secure in the active outsider attack model) if, for any probabilistic polynomial-time \mathcal{A} as above, it holds that $\text{Adv}_{\mathcal{A}}(\kappa)$ is negligible in κ .

Definition 6.4 (strong-security). Consider an adversary \mathcal{A} that gets to

1. Select adaptively $\mathcal{R}^{(1)}, \mathcal{R}^{(2)}, \dots, \mathcal{R}^{(\ell_1)}$ of receivers, obtain I_u for all $u \in \mathcal{R}^{(i)}$ and see $C^{(1)}, C^{(2)}, \dots, C^{(\ell_1)}$ for $i = 1, 2, \dots, \ell_1$.
2. Choose a message M as the challenge plaintext and a set \mathcal{R} of revoked users that must include all the ones it corrupted (but may contain more); i.e., $\cup_{i=1}^{\ell_1} \mathcal{R}^{(i)} \subseteq \mathcal{R}$. \mathcal{A} then receives an encrypted message C with a revoked set \mathcal{R} , where C is the encryption of either M or a random message of the same length. We may call this the “challenge” message.
3. Select adaptively $\mathcal{R}^{(\ell_1+2)}, \mathcal{R}^{(\ell_1+3)}, \dots$ of receivers and obtain I_u for all $u \in \mathcal{R}^{(i)}$ for $i = \ell_1 + 2, \ell_1 + 3, \dots$. Besides, \mathcal{A} may select messages $M^{(\ell_1+2)}, M^{(\ell_1+3)}, \dots$ and see the encryption of $C^{(\ell_1+2)}, C^{(\ell_1+3)}, \dots$.

Now \mathcal{A} has to guess whether C corresponds to the encryption of the real message M or a random message. Denote by **Succ** the event that \mathcal{A} makes the right guess. The advantage of \mathcal{A} is defined as $\text{Adv}_{\mathcal{A}}(\kappa) = |2 \cdot \Pr[\text{Succ}] - 1|$, where $\Pr[\text{Succ}]$ is the probability that the event **Succ** occurs, and the probability is taken over the coins used by the center and by \mathcal{A} . We say that a stateless group communication scheme is *strongly-secure* (or backward-secure in the active outsider attack model) if, for any probabilistic polynomial-time \mathcal{A} as above, it holds that $\text{Adv}_{\mathcal{A}}(\kappa)$ is negligible in κ .

Definition 6.5 (forward-security in the passive attack model). Consider an adversary \mathcal{A} that gets to

1. Select adaptively $\mathcal{R}^{(1)}, \mathcal{R}^{(2)}, \dots, \mathcal{R}^{(\ell_1)}$ of receivers, and see $C^{(1)}, C^{(2)}, \dots, C^{(\ell_1)}$ for $i = 1, 2, \dots, \ell_1$. However, \mathcal{A} does not have access to any I_u , where $u \in \mathcal{R}^{(i)} \setminus \{\mathcal{A}\}$ and $i = 1, 2, \dots, \ell_1$.
2. Choose a message M as the challenge plaintext and a set \mathcal{R} of revoked users that must include all the ones it corrupted (but may contain more); i.e., $\cup_{i=1}^{\ell_1} \mathcal{R}^{(i)} \subseteq \mathcal{R}$. \mathcal{A} then receives an encrypted message C with a revoked set \mathcal{R} , where C is the encryption of either M or a random message of the same length. We may call this the “challenge” message.

Now \mathcal{A} has to guess whether C corresponds to the encryption of the real message M or a random message. Denote by **Succ** the event that \mathcal{A} makes the right guess.

The advantage of \mathcal{A} is defined as $\text{Adv}_{\mathcal{A}}(\kappa) = |2 \cdot \Pr[\text{Succ}] - 1|$, where $\Pr[\text{Succ}]$ is the probability that the event **Succ** occurs, and the probability is taken over the coins used by the center and by \mathcal{A} . We say that a stateless group communication scheme is *secure* (or forward-secure in the active outsider attack model) if, for any probabilistic polynomial-time \mathcal{A} as above, it holds that $\text{Adv}_{\mathcal{A}}(\kappa)$ is negligible in κ .

Definition 6.6 (backward-security in the passive attack model). Consider an adversary \mathcal{A} that gets to

1. Select adaptively $\mathcal{R}^{(1)}, \mathcal{R}^{(2)}, \dots, \mathcal{R}^{(\ell_1)}$ of receivers, and see $C^{(1)}, C^{(2)}, \dots, C^{(\ell_1)}$ for $i = 1, 2, \dots, \ell_1$. However, \mathcal{A} does not have access to any I_u , where $u \in \mathcal{R}^{(i)} \setminus \{\mathcal{A}\}$ and $i = 1, 2, \dots, \ell_1$.
2. Choose a message M as the challenge plaintext and a set \mathcal{R} of revoked users that must include all the ones it corrupted (but may contain more); i.e., $\cup_{i=1}^{\ell_1} \mathcal{R}^{(i)} \subseteq \mathcal{R}$. \mathcal{A} then receives an encrypted message C with a revoked set \mathcal{R} , where C is the encryption of either M or a random message of the same length. We may call this the “challenge” message.
3. Select adaptively $\mathcal{R}^{(\ell_1+2)}, \mathcal{R}^{(\ell_1+3)}, \dots$ of receivers, and possibly select messages $M^{(\ell_1+2)}, M^{(\ell_1+3)}, \dots$ and see the encryption of $C^{(\ell_1+2)}, C^{(\ell_1+3)}, \dots$. However, \mathcal{A} does not have access to any I_u , where $u \in \mathcal{R}^{(i)} \setminus \{\mathcal{A}\}$ and $i = \ell_1 + 2, \ell_1 + 3, \dots$.

Now \mathcal{A} has to guess whether C corresponds to the encryption of the real message M or a random message. Denote by **Succ** the event that \mathcal{A} makes the right guess. The advantage of \mathcal{A} is defined as $\text{Adv}_{\mathcal{A}}(\kappa) = |2 \cdot \Pr[\text{Succ}] - 1|$, where $\Pr[\text{Succ}]$ is the probability that the event **Succ** occurs, and the probability is taken over the coins used by the center and by \mathcal{A} . We say that a stateless group communication scheme is *strongly-secure* (or backward-secure in the active outsider attack model) if, for any probabilistic polynomial-time \mathcal{A} as above, it holds that $\text{Adv}_{\mathcal{A}}(\kappa)$ is negligible in κ .

It is trivial to see that *strong-security* implies *backward-security in the passive model*, and that *security* implies *forward-secure in the passive attack model*.

6.2. Relationships between the security notions

We summarize the relationships between the security notions of stateless group communication schemes in Fig. 7, where $X \rightarrow Y$ means X is stronger than Y , $X \leftrightarrow Y$ means X is equivalent to Y , $X \not\rightarrow Y$ means X does not imply Y , and $X \stackrel{?}{\rightarrow} Y$ means it is unclear where X implies Y . Below we elaborate on the non-trivial relationships showed in Fig. 7.

Proposition 6.1. *If a stateless group communication scheme is strongly-secure, then it is also secure.*

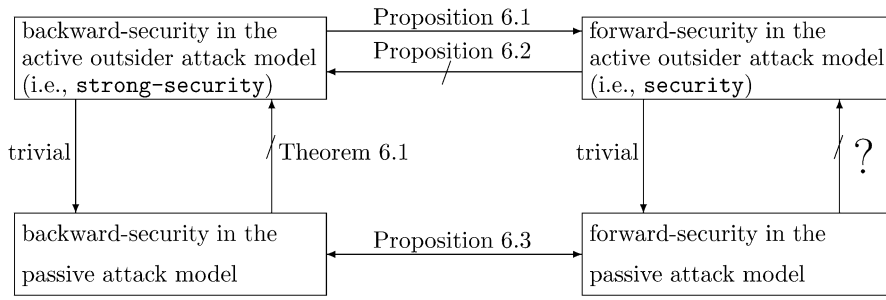


Fig. 7. The relationships between the security notions in stateless group communication schemes.

Proof. This is almost immediate because, on one hand, the definition of strong-security ensures the secrecy of the encrypted content of C even if \mathcal{A} can have access to I_u for $u \in \mathcal{N} \setminus \mathcal{R}^{(i)}$ for $i = \ell_1 + 2, \ell_1 + 3, \dots$, and on the other hand, the definition of security ensures the secrecy of the encrypted content of C only if \mathcal{A} does not have access to any I_u such that $u \in \mathcal{N} \setminus \mathcal{R}^{(i)}$ and $i \in \{\ell_1 + 2, \ell_1 + 3, \dots\}$. \square

Proposition 6.2. A stateless group communication scheme that is secure is not necessarily strong-secure.

Proof. The fact that security does not imply strong-security is implied by (1) Theorem 6.3, which states that the complete subtree method of the subset-cover framework is secure, and (2) that the subset-cover framework is insecure against an active outsider attacker (cf. the attack scenario in Section 1.1). The key observation is indeed that the adversary’s capability in the strong-security is strictly stronger. \square

The above proposition implies that for a stateless group communication scheme, one only needs to show that it is strongly-secure.

Proposition 6.3. A stateless group communication scheme is backward-secure in the passive attack model iff it is forward-secure in the passive attack model.

Proof. First we show that a stateless group communication scheme that is not forward-secure in the passive attack model is also not backward-secure in the passive attack model. Suppose \mathcal{A} is legitimate with respect to $C^{(i_1)}$, and illegitimate with respect to $C^{(i_2)}$ where $i_1 < i_2$. Since the scheme is not forward-secure in the passive attack model, \mathcal{A} can derive some information about M corresponding to the $(\ell_1 + 1)$ th broadcast C with a non-negligible probability, where $i_2 \leq \ell_1 + 1$. Now suppose \mathcal{A} is legitimate with respect to $C^{(i_3)}$ where $\ell_1 + 1 < i_3$. Then, with respect to $C^{(i_3)}$, \mathcal{A} can derive some information about a past encrypted message M with respect to the $(\ell_1 + 1)$ th broadcast with a non-negligible probability. Since \mathcal{A} does

1 not corrupt any other legitimate user $u \in \mathcal{R}^j \setminus \{\mathcal{A}\}$ for $j = \ell_1 + 2, \ell_1 + 3, \dots$, the
 2 scheme is not backward-secure in the passive attack model.

3 Second we show that a group communication scheme that is not backward-secure
 4 in the passive attack model is also not forward-secure in the passive attack model.
 5 Suppose $\mathcal{A} \in \mathcal{N} \setminus \mathcal{R}_{i_1}$, $\mathcal{A} \notin \mathcal{N} \setminus \mathcal{R}_{i_2}$, and $\mathcal{A} \in \mathcal{N} \setminus \mathcal{R}_{i_3}$, where $i_1 < i_2 < i_3$.
 6 Since the scheme is not backward-secure in the passive attack model, without loss of
 7 generality, \mathcal{A} can derive some information about $M^{(i)}$ for some $i_2 \leq i < i_3$ with a
 8 non-negligible probability. This also means that, with respect to $C^{(i_2)}$, \mathcal{A} can derive
 9 some information about a future message $M^{(i)}$ for some $i \geq i_2$. Since \mathcal{A} does not
 10 corrupt any other legitimate users, the scheme is not forward-secure in the passive
 11 attack model. \square

12
 13 We do not know whether forward-security in the passive attack mode also implies
 14 forward-security in the active outsider attack model. The relationship may seem trivial
 15 at a first glance, since all the corrupt members are revoked before the “challenge”
 16 session, and the adversary is not allowed to corrupt any member after the “challenge”
 17 session. Although it can indeed be shown that the implication holds, provided that
 18 the adversary is *static* (meaning that the adversary decides which principals in \mathcal{N} it
 19 will corrupt), in the more interesting case that the adversary is *adaptive*, we do not
 20 know how to prove it.

21
 22
 23 **Theorem 6.1.** *There exists a stateless group communication scheme that is*
 24 *“backward-secure in the passive attack model” but not strongly-secure (i.e.,*
 25 *backward-secure in the active outsider attack model).*

26
 27 **Proof.** Theorem 6.3 shows that the complete subtree revocation scheme in the
 28 subset-cover framework is *secure* (i.e., forward-secure in the active outsider at-
 29 tack model), which trivially means that it is also forward-secure in the passive attack
 30 model. Then, Proposition 6.3 shows that it is also backward-secure in the passive
 31 attack model.

32 On the other hand, the attack scenario showed in Section 1.1 states that the subset-
 33 cover framework is not backward-secure in the active outsider attack model. \square

34 6.3. A compiler for stateless group communication schemes

35
 36
 37 Now we present a compiler that can transform a subclass of *secure* stateless
 38 group communication schemes falling into the subset-cover framework (called the
 39 input schemes) into *strongly-secure* ones. The subclass of stateless group
 40 communication schemes has the characteristics that the different keys belonging to
 41 $\{L_i\}_i \cup \{I_u\}_u$ are computationally independent of each other. Let $\{f_k\}$ be a pseudo-
 42 random function family. The compiler is specified in Fig. 8.

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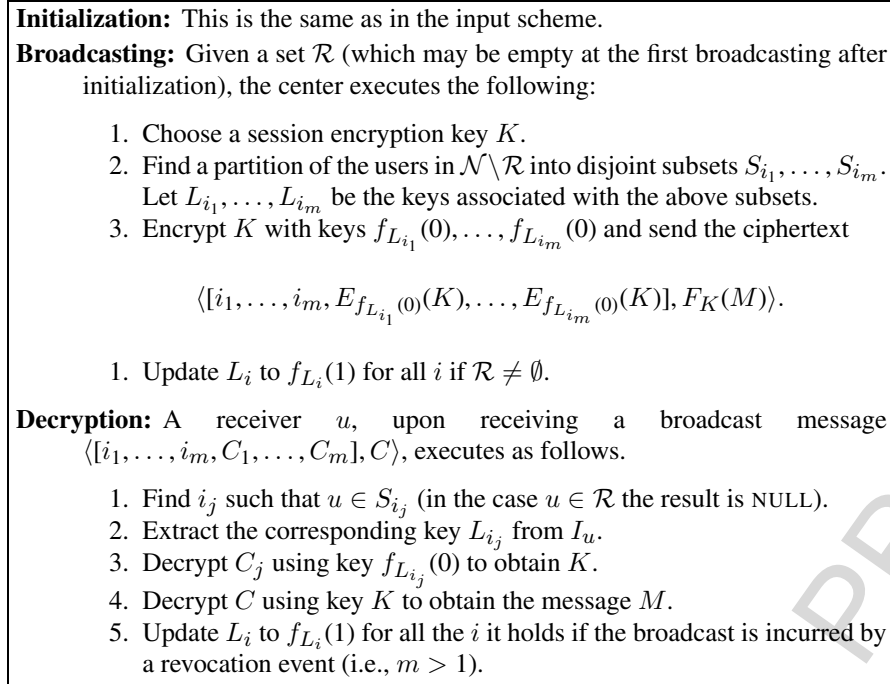


Fig. 8. The compiler for stateless group communication schemes.

6.4. Security analysis of the compiler

The key idea that the scheme resulting from the above compiler is not subject to the attack presented in the introduction is the following: compromise of a user at time t does not allow the adversary to recover keys corresponding to time $t_1 < t$. This is fulfilled by updating the keys using an appropriate family of pseudorandom functions.

Theorem 6.2. *Suppose the input scheme is secure, and $\{f_k\}$ is a secure pseudorandom function family, and the different keys belonging to $\{L_i\}_i \cup \{I_u\}_u$ are computationally independent of each other. Then, the above scheme is strongly-secure in the sense of Definition 6.4.*

Proof. Consider a mental game in which the system is initialized as in the input scheme. However, with respect to each broadcast operation, each incorrupt L_i is substituted with a pair of independently chosen random keys $\langle L_i^{(a,0)}, L_i^{(a,1)} \rangle$ such that $L_i^{(a,0)}$ is used to encrypt the message-encryption key K (if selected), where $a = 1, 2, \dots$. We claim that this scheme is secure. This is because the keys that

are used to encrypt the session key are freshly and independently chosen at random, which means that it is essentially a “short-lived” version of the input scheme. We also claim that this scheme is *strongly-secure*. This is because the keys that are used to encrypt the message-encryption key are freshly and independently chosen at random, which means that the secrets compromised after the “challenge” message are information-theoretically independent of the secrets used to encrypt the session key in the “challenge” message. Therefore, this scheme is *strongly-secure*.

Suppose the scheme output by the compiler (called the real-life scheme) is not *strongly-secure*. We observe that the difference between the above mental game and the real-life scheme is “how the incorrupt keys are evolved.” Specifically, for $a > 0$, in the former case, the $\langle L_i^{(a,0)}, L_i^{(a,1)} \rangle$ are independently chosen at random; in the latter case, $\langle L_i^{(a,0)} = f_{f_{L_i^{(j,1)}}^{a-1}}(0), L_i^{(a,1)} = f_{L_i^a}^a(1) \rangle$, where $f_X^0(\cdot) = X$, $f_X^1(\cdot) = f_X(\cdot)$, and $f_X^2(\cdot) = f_{f_X(\cdot)}(\cdot)$.

Now we consider the following experiment EXPT_j , where $0 \leq j \leq \ell$ and ℓ is the total number of revocation operations (which is polynomially bounded). The experiment is initialized as in the above mental game or as in the real-life scheme (both are the same at this stage). For any $0 \leq a \leq j$, any *incorrupt* $\langle L_i^{(a,0)}, L_i^{(a,1)} \rangle$ are independently chosen at random. For any $j < a \leq \ell$, any *incorrupt* $\langle L_i^{(a,0)}, L_i^{(a,1)} \rangle$ is defined as $\langle L_i^{(a,0)} = f_{f_{L_i^{(j,1)}}^{a-j-1}}(0), L_i^{(a,1)} = f_{L_i^{(j,1)}}^{a-j}(1) \rangle$. The experiments can get through because the secrets (some of them are used for encrypting the message-encryption key) are (at least) computationally independent of each other. We observe that EXPT_0 corresponds to the real-life scheme, and EXPT_ℓ corresponds to the above mental scheme. Since we assumed that EXPT_0 is not *strongly-secure*, it holds that \mathcal{A} has a non-negligible success probability ε_0 with respect to Definition 6.4. On the other hand, we already know that EXPT_ℓ is *strongly-secure*, which means that \mathcal{A} has only a negligible success probability ε_ℓ . Since ℓ is polynomially bounded, there must exist $0 \leq j < \ell$ such that EXPT_j and EXPT_{j+1} are distinguishable with a non-negligible probability (by the means of the adversary \mathcal{A} that may or may not break the *strong-security* in the respective experiments). Suppose f is a challenge oracle that is either a random function or a pseudorandom function with equal probability. Then, we can distinguish a random function from a pseudorandom one, via black-box access to f , with a non-negligible probability by letting $\langle L_i^{(j,0)}, L_i^{(j,1)} \rangle$ be obtained from an oracle query to f with respect to $L_i^{(j-1,1)}$. \square

6.5. A concrete *strongly-secure stateless group communication scheme*

Within the subset-cover revocation framework, [22] presented two concrete algorithms, namely the *complete subtree method* and the *subset difference method*. The difference between the two methods is how the collection of subsets (covering $\mathcal{N} \setminus \mathcal{R}$) is selected. Now we briefly review the *complete subtree method*, to which the above compiler is applicable.

1 Suppose the receivers are the leaves in a rooted full binary tree with N leaves 1
 2 (assume that N is a power of 2). Such a tree contains $2N - 1$ nodes (leaves plus 2
 3 internal nodes) and for any $1 \leq i \leq 2N - 1$ we assume that v_i is a node in the 3
 4 tree. Denote by $ST(\mathcal{R})$ the unique (directed) Steiner Tree induced by the set \mathcal{R} or 4
 5 vertices and the root; i.e., the minimal subtree of the full binary tree that connects all 5
 6 the leaves in \mathcal{R} . The collection of subsets S_1, \dots, S_w in this scheme corresponds to 6
 7 all complete subtrees in the full binary tree. For any node v_i in the full binary tree 7
 8 (either an internal node or a leaf, $2N - 1$ altogether) let subset S_i be the collection 8
 9 of receivers u that correspond to the leaves of the subtree rooted at node v_i . In other 9
 10 words, $u \in S_i$ iff v_i is an ancestor of u . 10

11 The **initialization** algorithm is simple: assign an *independent* and random key 11
 12 L_i to every node v_i in the complete tree, and provide every receiver u with the 12
 13 $\log N + 1$ keys associated with the nodes along the path from the root to leaf u . (As 13
 14 said before, if the secret information I_u is transmitted using a key established via a 14
 15 two-party authenticated key-exchange protocol, then the key is securely erased after 15
 16 the initialization.) The **broadcasting** algorithm is as follows. For a given set \mathcal{R} of 16
 17 revoked receivers, let u_1, \dots, u_r be the leaves corresponding to the elements in \mathcal{R} . The 17
 18 method to partition $\mathcal{N} \setminus \mathcal{R}$ into disjoint subsets is as follows. Let S_{i_1}, \dots, S_{i_m} be all 18
 19 the subtrees of the original tree that “hang” off $ST(\mathcal{R})$; i.e., all subtrees whose roots 19
 20 v_1, \dots, v_m are adjacent to nodes of outdegree 1 in $ST(\mathcal{R})$, but are not in $ST(\mathcal{R})$. It 20
 21 follows immediately that this collection covers all nodes in $\mathcal{N} \setminus \mathcal{R}$ and only those. 21
 22 As a result, in the **decryption** algorithm, given a message 22

$$\langle [i_1, \dots, i_m, E_{L_{i_1}}(K), \dots, E_{L_{i_m}}(K)], F_K(M) \rangle$$

23 a receiver u needs to find whether any of its ancestors is among i_1, \dots, i_m ; note that 23
 24 there can be only one such ancestor, so u may belong to at most one subset. 24
 25

26 Note that the number of subsets in a cover with N users and r revocations is at 26
 27 most $r \log(N/r)$. The message length is of at most $r \log(N/r)$ keys. Each receiver 27
 28 stores $\log N$ keys, and the center stores $2N - 1$ keys. The decryption process in- 28
 29 curs $O(\log \log N)$ comparison operations (for finding the cover) plus two decryption 29
 30 operations. 30
 31

32 Proof of the following theorem can be straightforwardly adapted from [22]. 32
 33

34 **Theorem 6.3.** *The complete subtree revocation scheme of the subset-cover frame-* 34
 35 *work is secure.* 35
 36

37 As showed before, the subset-cover framework, and thus the complete subtree 37
 38 revocation scheme, is not strongly secure. As a corollary of Theorem 6.2 38
 39 (which states that the compiler in Section 6.3 can transform a secure state- 39
 40 less group communication scheme into a strongly-secure one) and Theo- 40
 41 rem 6.3 (which states that the above complete subtree method is a secure stateless 41
 42 group communication scheme), the scheme output by the compiler is strongly- 42
 43 secure. 43

1 **Corollary 6.1.** *The stateless group communication scheme obtained by applying the*
 2 *compiler in Section 6.3 to the above secure complete subtree revocation scheme*
 3 *is strongly-secure.*

4
 5 Now we analyze the *extra* complexities (corresponding to each revocation event)
 6 for achieving strong-security.

- 7 • The center updates its keys by evaluating $2N - 1$ pseudorandom functions (this
 8 corresponds to the worst case scenario that no keys have been corrupt – the corrupt
 9 keys, if known, do not need to be updated). Moreover, in order to encrypt
 10 a message, the center needs to evaluate $r \log(N/r)$ pseudorandom functions;
 11 this computational complexity can indeed be traded with an extra $2N - 1$ stor-
 12 age complexity. Since the center is typically powerful in terms of computation,
 13 communication, and storage, these extra complexities are insignificant.
- 14 • Each receiver needs to evaluate $2 \log N$ pseudorandom functions and at most
 15 stores $\log N$ keys. Even if the receivers are low-end equipment (e.g., sensors),
 16 these extra complexities should still be insignificant.

18 6.6. Discussions

19
 20 The class of the stateless group communication schemes that can be made
 21 strongly-secure via the compiler in Section 6.3 should possess the following
 22 property: all the different keys belonging to $\{L_i\}_i \cup \{I_u\}_u$ are computationally-
 23 independent of each other. This explains why the above compiler applies to the
 24 *complete subtree method* of [22]. On the other hand, the *subset difference method*
 25 of [22], which does not achieve the desired strong-security, cannot made
 26 strongly-secure via the above compiler because the keys belonging to $\{L_i\}_i \cup$
 27 $\{I_u\}_u$ are not computationally independent.⁴

28 The stateless group communication schemes presented in [12], which outperforms
 29 [11,22] under certain interesting circumstances, are not strongly-secure. Un-
 30 fortunately, they cannot be made strongly-secure via the above compiler for
 31 a similar reason. It is an interesting open question to make the stateless group com-
 32 munication schemes of [12] strongly-secure at an expense similar to the extra
 33 complexity imposed by the compilers presented in this paper.

36 7. Conclusion and open problems

37
 38 We showed that a class of existing group communication schemes, stateful and
 39 stateless alike, are vulnerable to a realistic severe attack. We presented formal models
 40 that allow us to capture the desired security properties, and explore the relationships

41
 42 ⁴The independence condition can indeed be satisfied at the expense of each receiver storing $O(N)$ keys,
 43 which is clearly not scalable.

1 between the security notions. We showed how some methods can make a *subclass* of
 2 existing schemes immune to the attack at a very small extra cost. An interesting open
 3 question is to make other schemes (e.g., the stateful [2,25] and the stateless [12])
 4 secure against the attack without imposing any significant extra complexity.

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 13

15 Join protocol for group-oriented rekeying: // suppose user u joins the group
 16 server s generates a new key k_u for user u
 17 server s finds a joining point x_j
 18 server s attaches k_u to x_j
 19 let x_0 be the root
 20 $\bar{k}_{j+1} \leftarrow k_u$
 21 denote by x_{i-1} the parent of x_i for $1 \leq i \leq j$
 22 let $\bar{k}_0, \bar{k}_1, \dots, \bar{k}_j$ be the current keys of x_0, \dots, x_j , respectively
 23 server s generates fresh keys $\hat{k}_0, \hat{k}_1, \dots, \hat{k}_j$ // new keys of x_0, \dots, x_j
 24 $s \rightarrow \text{USERSET}(\bar{k}_0) : \{\hat{k}_0\}_{\bar{k}_0}, \{\hat{k}_1\}_{\bar{k}_1}, \dots, \{\hat{k}_j\}_{\bar{k}_j}$
 25 $s \rightarrow u : \{\hat{k}_0, \hat{k}_1, \dots, \hat{k}_j\}_{k_u}$
 26

27 Leave protocol for group-oriented rekeying: // suppose u leaves the group
 28 let x_{j+1} be the deleted k -node for k_u
 29 $\bar{k}_{j+1} \leftarrow k_u$
 30 server s finds the leaving point x_j (parent of k_u)
 31 server s removes \bar{k}_{j+1} from the key tree
 32 let x_0 be the root
 33 denote by x_{i-1} the parent of x_i where $1 \leq i \leq j$
 34 let $\bar{k}_0, \bar{k}_1, \dots, \bar{k}_j$ be the keys of x_0, x_1, \dots, x_j // they need to be changed
 35 server s generates fresh keys $\hat{k}_0, \hat{k}_1, \dots, \hat{k}_j$ as the new keys of x_0, x_1, \dots, x_j
 36 FOR $i = 0$ TO j
 37 let $\bar{k}_{i_1}, \dots, \bar{k}_{i_{z_i}}$ be the keys at the children of x_i in the new key tree
 38 $L_i \leftarrow (\{\hat{k}_i\}_{\bar{k}_{i_1}}, \dots, \{\hat{k}_i\}_{\bar{k}_{i_{z_i}}})$
 39 $s \rightarrow \text{USERSET}(\bar{k}_0) \setminus \{u\} : (L_0, \dots, L_j)$
 40
 41
 42
 43

Fig. 9. Join- and leave-incurred group-oriented rekeying in LKH.

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4 4
5 5

6 Appendix A. Join and Leave Protocols of LKH 6 7 7

8 For completeness, we briefly review join and leave protocols of LKH in Fig. 9. 8
9 The notations are consistent with the main body of the paper. 9
10 10
11 11

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