

Mock Exam for Final Discrete Mathematical Structures CS3233

December, 2007

The final exam is cumulative. This mock exam covers material starting with that presented in lecture 11/13/2007, which was not previously tested. This includes material in sections 5.1, 5.2, 5.3 and 6.1. Students should refer to midterms 1 and 2, and to the corresponding mock exams and homeworks, for assistance in studying material previously tested.

Where numerical answers are requested, do not fully evaluate your expressions. Simplify your answers so that they are expressed in terms of factorials and exponents, but not in terms of $C(n, r)$ or $P(n, r)$. This is how you will answer this sort of question on the final.

1. How many r -letter words can be constructed using an alphabet of size n ?
2. How many ways are there to order a set of size n ?
3. How many ways are there to order a set of size n if the first r places are always occupied by the same r elements?
4. How many ways are there to partition a set of size n into two sets, one of which has size r ? (A *partition* of set S is a collection of subsets of S such that the intersection of any two sets in the collection is empty and the union of all the sets in the collection is the whole original set.)
5. How many ways are there to partition a set of size n into two sets A and B ? Note that it matters which set is called A and which one is called B .
6. How many 8-bit sequences have exactly 3 0's?
7. How many ways are there to put 6 keys on a circular key ring? The two sides of the ring are the same and the two sides of the keys are the same. (So both ring and keys are symmetrical.) There is also no way to tell which key is first.
8. What is the probability of being dealt a particular hand of 5 cards from a deck of 52 distinct cards?
9. Suppose a permutation of all 26 lowercase letters is selected at random with each permutation equally likely.
 - (a) What is the probability that the first 13 letters of the permutation are in order?
 - (b) What is the probability that a and b are not next to each other?